

COMBAT RATION ADVANCED MANUFACTURING TECHNOLOGY DEMONSTRATION (CRAMTD)

"Dual-Use and Manufacturability"

Short Term Project (STP) #20

FINAL TECHNICAL REPORT

Results and Accomplishments (August 1994 through July 1995)

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1.0 CRAMTD STP #20

Results and Accomplishments

1.1 Introduction and Background

STP#20 started September 1, 1994 based on technical and cost proposals dated May 26, 1994 that were submitted to the DLA on May 31, 1994. Final approval for the project was received on August 30, 1994. The broad objective of the project was to develop and demonstrate a method for quantifying the manufacturability of products on food product filling and packaging systems and the flexibility of dual-use manufacturing. Indices were to be developed for manufacturability considering such factors as specification, production rate and product quality. Manufacturing characterization would support capital investment decisions leading to optimum flexibility and overlap with targeted products. Due to the time available, the scope was limited to MRE but can later be extended to Tray-Packs.

The military services express a need to make changes in the menu of combat rations (MRE) to minimize boredom among the soldiers who need to eat them. At present, the planned rate is about two entree items per year. The current growing requirement for using placeable food items instead of casserole items in MRE pouches is causing a significant change in the capital equipment needed. Changing from mechanically pumping food to individually placing relatively large items, such as smokey franks or chicken breasts requires a significant change in the kind of filling and packaging equipment that must be used. CRAMTD identified the horizontal form/fill/seal (HFFS) technology as an alternate packaging system with better capability to handle placeable type products. This project is to support assessment of potential MRE products as most suitable for this HFFS technology, and which are more difficult to manufacture. To make this assessment, a producibility index needs to be developed which measures the relative ease of manufacturing a product. Manufacturability measurement, in terms of a producibility index, is an essential part in the design process to determine the probability of successfully producing the product in terms of production rate, quality of final product, and the cost of production.

As described in STP #3, "Generic Inspection - Statistical Process Control System for a Combat Ration Manufacturing Facility" in the analysis of advanced process control strategies, if a process is poorly designed or the product has low producibility, the statistical parameters included in SPC control will be of little avail toward producing the desired quality. One of the objectives of STP #20 is to develop a measure of the ability of a food manufacturing process to produce products within a specified quality range.

1.2 Results and Conclusions

Following a literature search, investigation of potential MRE/Dual-Use products, processing capabilities, and measurement of product/process interactions, a producibility index was developed that includes process capability and manufacturing cost. The process capability index

component compares the quality of the produced products against the specification limits of the product to obtain an assessment of the process performance in producing consistent product quality. It, therefore, fulfills the objective of supporting Statistical Process Control in manufacturing quality management.

A cost analysis model, using commercially available spreadsheet software, of an MRE producing facility was developed that can be used to analyze the financial impact of various process option/configurations on the manufacturing cost of an MRE. This model provides the manufacturing cost input to the overall producibility index. Further, a systems dynamics model was developed to provide a visualization of the relationships between the various cost facets.

Finally the use of the producibility index was demonstrated in five case studies including Beef Stew and Ham Slice. The methodology and results are documented in Technical Working Paper (TWP) 106, "A Producibility Index with Process Capability and Manufacturing Cost", and are summarized in this Final Technical Report.

1.3 Recommendations

The concepts and methods developed in this STP should be broadly communicated so that manufacturers, process designers, and product specifiers more clearly understand and appreciate the role and interactions necessary to control cost and product quality. In addition to the distribution of TWP #106 "A Producibility Index with Process Capability and Manufacturing Cost", it is proposed that a Workshop be held to introduce the subject. Technical presentations at Food Engineering and Manufacturing forums such as the Institute of Food Technologists (IFT) are also important to wide acceptance of the concepts. Technical presentations, including technical publications in Journals, allow peer review to sharpen, endorse and promulgate the technology.

In support of enabling the computation and use of manufacturability/producibility indicies, including the methodology for collecting the necessary data, it is recommended that a next generation of computer software tools be developed. The mathematics, lookup tables, and spreadsheets should all be integrated in order to facilitate use of the concepts. A generalized manual should also be developed to guide the practitioner through the requisite process/product analysis and data collection.

2.0 Program Management

STP #20 was a two-phase work activity. The two phases had the following general objectives:

- Phase I** Develop a manufacturability index which includes equipment performance, product and process interactions, and manufacturing cost.
- Phase II** Recommend and demonstrate the manufacturability of a selected product and recommend how manufacturability of product/process can be improved.

Phase I was to begin with Literature, Equipment and Product Surveys and if no existing manufacturability index was found for food products, an adaptation was to be made from indices that were developed for discrete parts manufacture. Investment analysis was to be included in the assessment of manufacturability. Based on the information gathered and the methodology developed, Phase II was to demonstrate the manufacturability determination for one or more products. The work activity and status are illustrated on the attached Figure 1, CRAMTD STP#20 "Dual-Use and Manufacturability", Time and Event Milestones (Appendix 4.1).

2.1 Summary of STP Accomplishments

- The results of a literature survey indicated that no manufacturability index was ever developed for food product packaging.
- In cooperation with the U.S. Army Natick Research, Development and Engineering Center, a list of 28 MRE Entrees were identified for evaluation of their manufacturability.
- Virtual or Distributed Manufacturing was proposed as a concept to increase production capacity for MRE pouches and to lower cost.
- Potential MRE/Dual-Use entree items (Beef Burritos, Chicken Wings, Franfurters, Beef Steaks and Beef Stew) were evaluated.
- A piston filler nozzle, specifically designed for products such as beef stew, was used to quantify variability in net and drain weights.
- A method for determining the "fit" or "match" of product/process or process/process was developed.
- A producibility index was developed that includes evaluation of process capability, production rate, and manufacturing cost.
- A process capability index was defined which compares the variability of the quality distribution against the specification limits of the product.
- A financial model for an MRE producing facility was developed using commercially available spreadsheet software.
- A cost model was developed to demonstrate and provide visualization of the

relationship between the various cost facets of a manufacturing process.

- The use of the producibility index was demonstrated based on experiments on the MRE line with Beef Stew and Ham Slices
- Technical Working Paper (TWP) 106 “A Producibility Index with Process Capability and Manufacturing Cost” was written and distributed.
- The concept of the producibility index and its impact on statistical process control was described at the January 10, 1996 “MRE Quality Working Group” meeting in Cincinnati.

3.0 Short Term Project Activities

3.1 STP Phase 1 Task

3.1.1 Literature Survey (Task 4.3.1.1)

A literature survey was conducted and the results indicated that no index of manufacturability has ever been developed for food product packaging. The preliminary results of the literature survey were presented at the annual Fall Meeting of the R&D Associates and released as technical working paper, TWP 96, “Capability and Manufacturability Measures”. Technical working paper TWP 106, “A Producibility Index with Process Capability and Manufacturing Cost” (Appendix 4.2) extends and summarizes those findings in its Introduction.

Among various types of production systems, the manufacturing/assembly industry appears to be the first to pioneer the implementation of the design-production integration concept. Bolz (1977) provides the design principles that help to improve the designed product’s producibility in terms of machining processes. These design principles are later developed into a concept called “Design For Manufacturability (DFM)” and “Design For Assembly(DFA)”. *However, the DFM and DFA approaches are specifically focused on the physical aspects of manufacturability and assemblability and largely ignore the process/product interaction as related to the product quality.*

Harry and Lawson (1992) appear to be the first to pioneer producibility research by looking at the process capability. Their work is later included in “Producibility Measurement Guidelines” by the Department of Navy. In Harry and Lawson’s work, the calculation procedures for evaluating the process capability have been very carefully crafted. *However, they do not include many concerns that we believe should be addressed in evaluating product producibility, specifically: quality characterizations, production capacity, and manufacturing cost.*

3.1.2 Equipment and Product Survey (Task 4.3.1.2)

3.1.2.1 Products Survey

In cooperation with the US Army Natick Research, Development and Engineering Center, a list of 28 MRE Meals were identified for consideration in the evaluation of manufacturability. These meals represent either meals that were contracted for during the past five years or are being

considered for a contract in the next three years (Appendix 4.3).

3.1.2.2 Equipment Survey

In general, the filling equipment for the MRE menu items can be divided into two categories: placeable items and pumpable items. Potential filling equipment was identified during the Pack Expo in Chicago on November 13 through 17, 1994 for the dual use type products that were being considered in this STP. A significant study of filling equipment was conducted during the execution of STP #2, "Filling Systems" (see Final Technical Report STP #2 - FTR 8.0). As universal feed systems, the robot for placeable products and the piston type filler for pumpable products were identified. Other filling equipment is available for products such as frankfurters but are too product specific.

To assess the dual use capability of the food industry in the U.S., assistance was requested of several providers of horizontal form/fill/seal machines and several retort manufacturers. The survey (Appendix 4.4) was aimed at determining the number of operational units and the general usage. Unfortunately, only one manufacturer responded and therefore no summary or conclusions were drawn. The lack of response is attributed to a concern in disclosing market share of equipment sales (considered proprietary information).

3.1.2.3 Virtual or Distributed Manufacturing

Horizontal form/fill/seal equipment is extensively used in the meat packaging industry. Clear evidence of this can be seen in the supermarket where sliced meat products and prepared meats such as hot dogs and sausages are packed in HFSS containers. Most meat packaging plants pack products under refrigerated temperatures and distribute them under the same conditions. Most meat packaging plants, however, have no retort capability, and would require significant capital to become a producer of shelf stable food products.

On the other hand, the producers who manufacture shelf stable food products don't have the meat preparation capability and buy the meat products from the meat packers, either frozen or refrigerated, and repack into retortable containers.

The concept proposed is for meat packers to directly pack the product in a retortable container (e.g. MRE pouch). This product would then be packed in cardboard boxes and shipped under refrigerated condition to a thermal processing facility. The product would be maintained at an internal temperature of 28 to 40F at all times until it is loaded into retorts at the thermal processing facility. Maximum time from packaging to retort loading can be 72 hours. The product has to be in the retort process within 2 hours after it leaves the refrigerated environment.

This concept would increase the production capacity for MRE pouches dramatically, without major capital investment from the government. A potential exists for lower cost product to the government. A meat packing operation has adequate facilities to rework product. In the case of ham slice production, the end pieces don't meet military specifications and cannot be packed. A meat packer would regrind these ham pieces and blend them into the next batch.

There are issues that need to be resolved in order for this concept to become a reality:

1. Is the concept agreeable to the USDA and the regulations that govern the thermal

processing industry?

2. Under whose USDA stamp would the product be distributed?

3.1.3 Development of Producibility Index (4.3.1.3)

3.1.3.1 Product Characterization

To test the manufacturability of a range of products, potential MRE/Dual-Use entree items (Beef Burritos, Chicken Wings, Frankfurters and Beef Stew) were evaluated in the CRAMTD plant. It was observed that the MRE packaging material is sensitive to "defined" objects, such as chicken drumsticks. Under high vacuum the pouch will stretch around these objects and possibly lead to a film failure. Beef Stew was evaluated as a model pumpable product, and capability studies were conducted to quantify the performance of various pumping systems.

The evaluation of potential MRE/Dual Use entree items was continued by evaluating the packaging of commercially available Beef Steaks. As was observed earlier, the MRE packaging material is sensitive to "defined" objects. In this case, the ice crystals on the surface of frozen beef steaks damaged the film, leading to the conclusion that these products need to be at least defrosted on the surface prior to packaging.

3.1.3.2 Process Capability

Emphasis was also placed on characterizing the capability index of a piston filler for pumpable product, such as beef stew. For this purpose, a plug nozzle specifically designed for such products was rented and experiments executed to quantify the variability in net weight, component weights and drain weight.

Four different measures of Process Capability are possible of which C_p is shown below (see TWP 106 for a complete description of this as well as the other measures). C_p is appropriate for those processes that can be adjusted to meet the target value and where distribution is normal:

$$C_p = \frac{USL - LSL}{6\sigma}$$

USL and LSL are the upper and lower specification limits respectively and the difference between them constitutes the tolerance for the quality characteristic being produced. Sigma, σ , is the standard deviation in the quality characteristic for the units produced by the available equipment. In order to obtain a high process capability index, one would like to see a high value for the tolerance (i.e., wide range of quality characteristic acceptability) and a low value for process standard deviation (i.e., well controlled process).

In the summary table below, a comparison of process capabilities is shown for two nozzles, standard and plug, and for manual filling. Process capability correlated with the standard deviation of the net fill weight (C_p assumes that the mean can be adjusted).

Table 3.1.3.2 Process Capability of Filling Beef Stew, Summary

Filler	Average Fill Weight	Std. Dev.	C_p
Standard Nozzle	222.8 g	5.23	0.89
Plug Nozzle	207.5	3.58	1.3
Manual Fill	233.8	3.09	1.5

3.1.3.3 Product/Process Measurements

Manufacturability of a product is a function of multiple “process” factors, such as packaging system, filling system, and the interactions between product and package. To quantify the manufacturability of a product/process system various “measurements” have to be conducted that relate the above system configuration to process efficiency, product yield, manufacturing cost, and other qualitative factors. One procedure has been developed to define the volume of the formed pouch and compare it to the volume of the product fill, with their respective standard deviations. The form of the Process Capability for “one-sided tail” comparisons C_{pk} is:

$$C_{pk} = \frac{\text{Container Volume} - \text{Product Volume}}{3\sigma}$$

Sigma, σ , is the estimated standard deviation for the difference in container and product volumes:

$$\sigma = \sqrt{(\sigma_{cnt}^2 + \sigma_{prd}^2)}$$

Using the standard deviations reported for section 3.1.3.2 filling but with a mean fill volume of 230cc for each filler plus a reserve container space of 65cc, and the pouch design volumes and standard deviations from TWP 106 (summarized in Table 3.1.3.3.a), the C_{pk} for the

combinations are shown in Table 3.1.3.3.b.

Table 3.1.3.3.a Pouch Volumes from TWP 106

Design	Pouch Film	Form Press.	Mean Vol.	Std Dev.
Pouch A	Reynolds	18 psi	261.5cc	5.80
Pouch B	Reynolds	22	318.0	7.89
Pouch C	Aluswiss	27	330.6	5.83
Pouch D	Aluswiss	24	306.5	5.30

Table 3.1.3.3.b Product/Process “fit”, C_{pk} .

Pouch	Standard Nozzle	Plug Nozzle	Manual Fill
Pouch A	-1.407	-1.622	-1.686
Pouch B	0.801	0.880	0.901
Pouch C	1.491	1.718	1.784
Pouch D	0.506	0.593	0.619

Given the volume of Pouch A along with the reserve space, none of the Pouch A product fills “fit” (C_{pk} is negative). The other combinations do “fit”. The rank order based on pouch volume is that associated with standard deviation rather than mean volume. Similarly, the order associated with filling is that based on standard deviation (but in the example shown the mean volume of fill was assumed to be the same).

In the above example, other variables such as particle size, density and viscosity were not taken into account. As a result, the actual values shown are not transferrable to other products. The subject of Product/Process Measurements and “fits” will continue to be explored.

3.1.2.4 Producibility Index

Following the evaluations of process capability and manufacturing cost a producibility index is proposed that includes these two evaluations.

The producibility index (PI) proposed has the following form:

$$PI = [PCI_{critical}, PCI_{major}, PCI_{minor}, PCI_{average}, MC].$$

This index takes into account the critical, major, and minor characteristics of the product, and the manufacturing cost (MC). Sensitivity studies helped in selecting the most adequate index to be used. The geometric mean is more sensitive to small values than the arithmetic mean. This is desireable because a smaller PCI value diminishes producibility considerably. A value of zero will result in a zero geometric mean regardless of how high other values are. This is also desireable since a process with a PCI value of zero for any one characteristic is considered absolutely unacceptable regardless of the quality level of other characteristics.

Process Capability Indices (PCI)

The Process Capability Index (PCI) is chosen instead of the more traditional measure, quality yield, because the modern quality control concept is no longer satisfied by the quality yield via intensive inspection efforts. "Yield" is simply a measure that indicates the percentage of the products produced that passes the tolerance gauge or meets the specifications. In contrast, PCI is an index that indicates the consistency of the product quality. It compares the variability of the quality distribution against the specification limits of the product to obtain a fair view of the process performance in producing consistent product quality.

As stated earlier (see discussion of Process Capability above and TWP 106), four different measures of the PCI are possible of which C_p is appropriate for those processes that can be adjusted to meet the target value and where the distribution is normal.

Manufacturing Cost Estimate (MC)

To estimate the manufacturing cost, the major elements taken into account were: production and schedule efficiency, raw materials, personnel, capital and equipment, and utilities. The values for MC are \$/unit. These elements are described and their computation demonstrated in TWP 106. They are presented as a guideline for manufacturing cost estimation but not the only elements to be considered. Practitioners should develop their own manufacturing costs based on their particular situation.

3.1.4 Investment Analysis (4.3.1.4)

A cost model of an MRE producing facility was developed that can be used to analyze the financial impact of various process options/configurations on the manufacturing cost of an MRE. The intent is that this model be used in conjunction with Non-traditional Capital Investment Criteria, which will be used to quantify the more subjective benefits of certain process configurations. This cost model was built within a spreadsheet software package and takes into account process factors such as line speed, line efficiency, product yield, labor cost, utility cost, raw material cost and capital investments. These models are demonstrated in TWP 106, see for example: page 34 and its appendix D for "Manufacturing Cost Analysis for Pouch Forming Design", page 38 and its appendix F for "Producibility Indices for Different Designs of the Target Fill Weight", and page 43 and its appendix G for "Producibility Index for the Ham Slice Pouches".

To visualize and demonstrate the relationships between various cost facets of a

manufacturing process, the same cost model was developed using “ithink” (High Performance Systems, Inc.) systems dynamics simulation software. The Systems Dynamics model is described in TWP 106, page 34 and its appendix E, “Visual Representation: Cost Analysis for Beef Stew Pouches”.

3.2 STP Phase II Task

3.2.1 Demonstration (Task 4.3.2.1)

In order to demonstrate the use of the developed producibility indices, experiments were conducted on the MRE line to produce Beef Stew and Ham Slices in MRE pouches under various product and process conditions. Data from these experiments are used as examples to demonstrate the use of the producibility index that was developed under this project (see attached TWP 106).

These experiments were targeted at demonstrating the application of the producibility index and did not include any adjustments in order to: a) optimize pouch forming (Pouch Forming Designs) nor b) optimize robot performance (Ham Slice Pouch). Conclusions drawn from these examples are, therefore, limited to the technologies as demonstrated in these experiments and not to the potential performance or even to our projected performance.

The cases used in the demonstration of Producibility Indices consisted of:

- A. Process/Product Design for Beef Stew MRE Pouches
 - 1. Pouch Forming Designs & Film
 - 2. Target Fill Weights
- B. Ham Slice MRE Pouches
 - 1. Hand Fill vs Robot Fill
 - 2. Automatic Slicing vs Automatic Slicing/Sizing.

3.2.2 Technical Guidance (4.3.2.2)

The Technical Working Paper TWP 106 “A Producibility Index with Process Capability and Manufacturing Cost” reviews current approaches to the assessment of product producibility and then develops and validates a methodology that quantifies the producibility of a product as it relates to its design characteristics. This TWP has been distributed as requested in response to the CRAMTD Abstract/Order Form.

The concept and its impact on Statistical Process Control was described at the January 10, 1996 “MRE Quality Working Group” meeting in Cincinnati.

The concepts and methods developed in this STP should be broadly communicated so that manufacturers, process designers, and product specifiers more clearly understand and appreciate the role and interactions necessary to controlled cost and quality product. In addition to the

distribution of TWP #106 "A Producibility Index with Process Capability and Manufacturing Cost", it is proposed that a Workshop be held to introduce the subject. Technical presentations at Food Engineering and Manufacturing forums such as the Institute of Food Technologists (IFT) are also important to wide acceptance of the concepts. Technical presentations, including technical publications in Journals, allow peer review to sharpen, endorse and promulgate the technology.

4.0 Appendix

- 4.1 Figure 1 CRAMTD STP #20 Time and Events Milestones**
- 4.2 Technical Working Paper (TWP) 106, “A Producibility Index with Process Capability and Manufacturing Cost”**
- 4.3 3-Year Outlook for MRE Entree Items**
- 4.4 Equipment Database Survey Form**

Figure 1 - CRAMTD Short Term Project #20
Dual-Use and Manufacturability
Projected Time & Events and Milestones

Task Name	Reference	1994			1995								
		Aug	Sep	Oct	Nov	Dec	Jan	Feb	Mar	Apr	May	Jun	Jul
Phase I													
Literature Survey	4.3.1.1												
Equipment and Product Survey	4.3.1.2												
Develop Man. Index	4.3.1.3												
Investment Analysis	4.3.1.4												
Phase II													
Demonstration	4.3.2.1												
Final Recommendation	4.3.2.2												

CENTER FOR ADVANCED FOOD TECHNOLOGY

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The following information was supplied by U.S. Army Natick Research, Development & Engineering Center on September 16, 1994

Products have been contracted for during the past four years (1991-1994):

MIL-B-44059	Beef Stew
MIL-C-44209	Chicken Stew
MIL-C-44210	Chicken with Rice
MIL-C-44204	Corned Beef Hash
MIL-E-44200	Escalloped Potatoes with Ham
MIL-F-44062	Frankfurters
MIL-H-44063	Ham Slice
MIL-O-44202	Omelet with Ham
MIL-P-44432	Pork Chow Mein
MIL-P-44201	Pork with Rice
MIL-S-44205	Spaghetti
MIL-T-44208	Tuna with Noodles

Proposed MRE Entree items for 1995 and 1996 are:

CID-A-A-20209	Beefsteak, grilled
MIL-B-44059	Beef Stew
CID-A-A-20207	Cheese Tortellini in Tomato Sauce
Draft CID	Chicken Parmesan
Draft MIL Spec	Chicken Patty, Grilled
MIL-C-44209	Chicken with Rice
MIL-C-44207	Chili and Macaroni
MIL-E-44200	Escalloped Potatoes with Ham
MIL-F-44062	Frankfurters
MIL-H-44063	Ham Slice
CID-A-A-20204	Pasta with Vegetables in Tomato Sauce
MIL-P-44432	Pork Chow Mein
MIL-P-44201	Pork with Rice
MIL-S-44205	Spaghetti
MIL-T-44208	Tuna with Noodles

MRE Developmental Items (no specification number assigned)

Beef Burrito
Biscuit
Corn Bread
Eggs, Hard-Poached
Fruit Chew Bar
Macaroni and Cheese
Pizza
Pork Rib in BBQ Sauce
Rice Pilaf
Waffles

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Equipment Data Base:

Under a contract with the Department of Defense, we need to assess the industrial capability of the food industry to produce combat ration products. To the best of our knowledge, your equipment is used or can be used in the production process of combat ration products. We would appreciate your cooperation in answering the questions below to the best of your knowledge

Equipment Vendor: _____

Name of Contact: _____

Title: _____

Address: _____

City _____ State: _____ Zip: _____

Telephone: _____ Fax: _____

Type of equipment used for filling / primary packaging / sterilization of entree items. Please indicate also how many units are operational in the food industry.

	Type	# Operational
1)	_____	_____
2)	_____	_____
3)	_____	_____

Break down of usage by type equipment

	1	%	2	%	3	%
Prepared Foods (dinners/meals/entrees)	_____	%	_____	%	_____	%
Prepared Meat, Poultry, Seafood	_____	%	_____	%	_____	%
Fruits and Vegetable Processing	_____	%	_____	%	_____	%
Bakery (fresh, refrigerated and frozen)	_____	%	_____	%	_____	%
Dairy/Beverage	_____	%	_____	%	_____	%

Note: The information supplied on this form will be shared with our contractor, the Department of Defense

COMBAT RATION ADVANCED MANUFACTURING TECHNOLOGY DEMONSTRATION (CRAIMTD)

A Productivity Index with Process Capability and Manufacturing Cost

Technical Working Paper (TWP) 106

E.A. Elsayed, H.B. Bruins, and A. Chen

September 1995

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A Producibility Index with Process Capability and Manufacturing Cost

Abstract

One of the important issues in product design is the assessment of its producibility at a required production rate and an acceptable cost. In this technical report, we review current approaches and then develop and validate a methodology that quantifies the producibility of a product as it relates to its design characteristics. This measure of producibility aims to assure that newly designed products can meet both quality and cost requirements. The measure integrates initial design ideas with actual production concerns and shortens the time required for introducing a new product to the market. It also provides information on the dual use of existing production technologies and facilities for both civilian and military products. This is especially useful for military specified products which are sub-contracted to civilian vendors.

1. Introduction:

A product life cycle roughly consists of three phases: product/process design, actual production, and post-production service and support. Traditionally, the early design phase of a product rarely interacts with other downstream phases. However, these downstream phases, such as the actual production and the after-sale customer service, are the phases that actually constitute the major cost of a product during its life cycle. Consequently, a product designed without integrating downstream concerns often requires additional redesigns due to unexpected high manufacturing cost or over-burdened post-production supports. For military products, a nonintegrated design also results in the inflexibility of military logistic mobilization because of the difficulties in converting civilian production facilities to produce military products.

In recognizing the great impact of the design phase on the latter phases and thus on the product life cycle, researchers propose various approaches to integrate the different phases of the life cycle. Feigenbaum (1961) proposed a *Total Quality Control System (TQCS)* where quality control activities are involved in every phase of the product life cycle. Through the common goal of achieving better quality, communications among company divisions are established and the integration of the product life phases becomes essential. Most recently, the *Concurrent Engineering (CE)* (Carter and Baker (1992)) approach specifically integrates different functional divisions and groups that are involved in the product life cycle. The approach has been further enhanced by devising a centralized Data Base Management System (DBMS). This approach

utilizes modern technologies of structural information systems (e.g., Wang (1993)) to establish a highly automatic information collecting and exchanging system. Through this information system, the integration can be achieved more effectively.

As discussed above, the conceptual framework is well established. However, the actual implementation is still in its infant stage. In this technical report, we particularly focus on the implementation methodologies for the integration of both the design phase and the production phase of the product. In the past, product design and production were performed by two separate groups of engineers. In fact, engineers from the two groups received very different disciplines and often had very distinctive, if not conflicting, concerns in the development and production of a product. For example, design engineers tend to focus on the performance and aesthetic aspects of the product while the production/process engineers are most concerned with the easing and streamlining of the product production. When these two groups of engineers do not cooperate in both the design and production activities, we often see either a newly designed product that is impossible or too costly to produce or a production process that is incapable of producing the desired product quality. The purpose of this report is to find a link that allows design engineers to validate their design and production engineers to ease the production set up procedures. We refer to this link between design and production engineers as the *Producibility Index (PI)* which provides a quantified index that takes into account both the quality and cost requirements for producing the products.

Among various types of production systems, the manufacturing/assembly industry appears to be the first to pioneer the implementation of the design-production integration concept. Traditionally, *manufacturing/assembly* is usually referred to as machine tooling type of production processes which fabricates required parts, that are later assembled together to construct the final product. Bolz (1977) provides the design principles that help to improve the designed product's producibility in terms of machining processes. Since the dramatic development of computer technologies in the 80's, production of computer components quickly gained the attentions of manufacturers. Clark (1989) proposes similar design principles for printed circuit boards. These design principles are later derived into a concept called *Design For Manufacturability (DFM)* and *Design For Assembly (DFA)* (see Boothroyd and Dewhurst (1983), Dwivedi and Klein (1986), and Alting and Boothroyd (1994)). However, the DFM and DFA approaches are specifically focused on the physical aspects of manufacturability and assemblability and largely ignore the process/product interaction as related to the product quality.

Unlike the manufacturability and assemblability, *Producibility* provides a quantitative measure that is desirable to evaluate the producibility of the newly designed product by looking at the capability of processes. It should be noted that the processes, that will be used to facilitate the production, should be designed together with the product feature design, as part of the DFM and DFA principles. Now, the question is: what is the process that will be deemed as a *capable* process? While the process capability indices are intensively explored by many researchers (e.g. Kane (1986), Chan, Cheng and Spiring (1988), Bissell (1990) and Boyles (1991)) and are recently summarized in Kotz and Johnson (1993), Harry and Lawson (1992) appear to be the first to pioneer the producibility research by looking at the process capability. Their work is later included in *Producibility Measurement Guidelines* by the Department of the Navy.

In Harry and Lawson's work, the calculation procedures for evaluating the process capability have been very carefully crafted. However, it does not include many concerns that we believe should be addressed in evaluating product producibility. Specifically, there are three issues that we focus on in this report: quality characterizations, production capacity, and rate and product cost. We now explain these issues.

Before evaluating process capability, one should first recognize the quality characteristics of concern. We refer to this step as *quality characterization*. In the conventional calculations of process capability indices, one usually focuses on one particular quality characteristic of interest. In reality, one characteristic is not really enough to reflect the overall process performance since most production processes usually involve more than one important characteristic. Furthermore, there may exist interactions among different characteristics which make the evaluation of process capability difficult for practitioners. As a consequence, some researchers also pay attention to the multivariate process capability indices (e.g., Hubele, Shahriari, and Cheng (1989), and Mendieta, Saleh and Liu (1994)). The proposed multivariate capability indices are, however, doomed to remain theoretical spectacles due to the complexity and the mathematical intangibility. In contrast, we consider multiple characteristics by their effects on the product's functionality instead of their possible interactive relationships. We classify characteristics into three categories: critical, major, and minor. Each one has various influences on the product's functionality. Based on these three characteristics, we develop a more tangible measurement of process capability for multi-characteristic products.

The required production capacity is also an important criterion when evaluating a newly designed product's producibility. A new product development is usually backed by a thorough study of market demand under the principle of concurrent engineering. In the case of military

products, the amount of demand for certain products under certain situations is always the focus of logistic planning. In order for the requirement for the projected production process to be capable of meeting the market demand, the requirement should be considered in the earliest phases of the product life cycle, namely, the product/process design. Taking into account the production capacity of a projected process, one can easily observe that very often the process capability itself is a function of the production rate. In other words, the process capability is not constant over different production rates. In the actual production setting, the production rate is difficult to maintain at a constant level due to usual incidents such as changeovers of feed stock or shifts or even machine breakdown. To more objectively evaluate the overall process capability, different product rates and their corresponding process capabilities should be addressed.

Manufacturing cost is the third issue which we are considering in the producibility index. In the past, improving quality and reducing cost were considered two conflicting tasks. Not until the Japanese competition did American industries realize that the two can actually be achieved together. With the recent advancement of quality technology, some researchers even try to represent product quality in terms of dollars and use the overall cost as an objective function that needs to be minimized. We, however, believe that the product quality is difficult, if not impossible, to assess in terms of cost since poor product quality not only diminishes customers' goodwill impression, which is already difficult to measure, but also causes loss to the entire society (Taguchi, 1981). Recognizing this, we include in the proposed producibility index (PI) both the process capability index (PCI), which is the measure of process performance on product quality, and the manufacturing cost (MC) which estimates the physical cost for producing a unit of product.

The remainder of this report is organized into four sections. In Section 2, we discuss and review the methodologies used for evaluating process capability. We review four common process capability indices (PCI's): C_p , C_{pk} , C_{pm} , and C^*_{pm} , and discuss their uses for different circumstances. Section 3 is devoted to the estimate of the manufacturing cost (MC) where the following are considered: production rate, process efficiency (yield), material cost, labor cost, utility cost, and capital cost. In Section 4, we propose a producibility index (PI) that takes into account both the quality of the product and its cost. The new index is also developed with regard to the quality characterization and the production capacity requirement. Finally, we demonstrate the proposed producibility index using examples from process designs for military combat rations: beef stew and ham slice MRE pouches.

2. Process Capability Indices (PCI)

In this section, we review several process capability indices (PCI's) that we will use later in the producibility study. The PCI is chosen instead of the more traditional measure, quality yield, because the modern quality control concept is no longer satisfied by the high quality yield via intensive inspection efforts. "Yield" is simply a measure that indicates the percentage of the products produced that passes the tolerance gauge or meets the specifications. In contrast, PCI is an index that indicates the consistency of the product quality. Figure 1 clearly illustrates this idea.

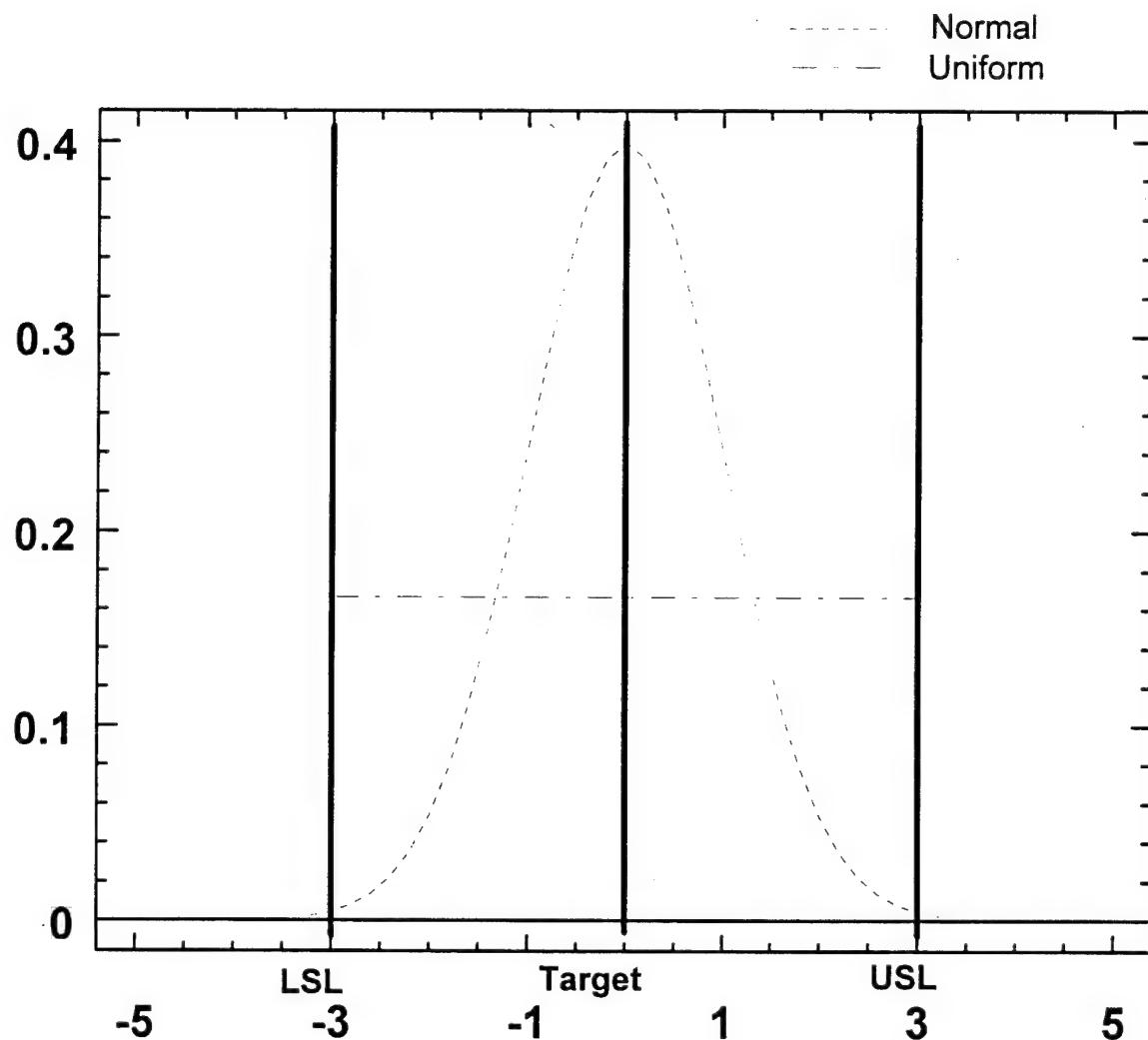


Figure 1: Comparison between the normal and uniform distributions

As shown in the Figure 1, the product characteristic being measured has a target value at 0 and lower and upper specification limits (LSL and USL) at -3 and 3, respectively. There are also two probability distributions shown in Figure 1: one is a uniform distribution, $U[-3,3]$, ranging from -3 to 3; and the other is a normal distribution, $N[0, 1]$, with mean 0 and standard deviation 1. It can be clearly observed from Figure 1 that the process with uniform distribution will have 100% yield since all products produced are within the specification limits. On the other hand, the process with normal distribution will only produce 99.73% yield. Nevertheless, the normal distribution clearly produces more consistent product quality since the distribution is more concentrated around the target. Thus, for the purpose of reflecting the quality consistency, yield is certainly not a good measure.

Process Capability Index (PCI) is invented to serve this purpose. It compares the variability of the quality distribution against the specification limits of the product to obtain a fair view of the process performance in producing consistent product qualities. In other words, PCI is more suitable for the modern quality control efforts that focus on reducing the variation of product quality instead of meeting the product specifications.

In this section, we will introduce four PCI measures: C_p , C_{pk} , C_{pm} , and C_{pm}^* that will be used later for the producibility study.

2.1 Process Capability Index C_p

The process capability measure C_p is the most widely used index. It is expressed as:

$$C_p = \frac{USL - LSL}{6\sigma}$$

To show how this measure effectively reflects the quality consistency, let us calculate the C_p values for the uniform distribution and for the normal distribution as shown in Figure 1. For the uniform distribution $U[-3, 3]$:

$$C_p(U[-3,3]) = \frac{3 - (-3)}{6(1.733)} = 0.577 ,$$

where the standard deviation for the distribution $U[-3,3]$ is 1.733. It can be seen that this C_p value is significantly lower than that for the normal distribution $N(0, 1)$:

$$C_p(N[0,1]) = \frac{3 - (-3)}{6(1.0)} = 1.0 ,$$

The yield for the uniform distribution is 100% and that for normal distribution is 99.73%. Since we are concerned with the product quality consistency, the C_p measure appears to be much better than the yield. It should be noted that the yield is still considered in our producibility index. However, it is considered a factor in estimating the manufacturing cost rather than being an element of the product quality.

To estimate C_p , the standard deviation (σ) is estimated as:

$$\hat{\sigma} = s = \sqrt{\frac{\sum_{i=1}^n (X_i - \bar{X})^2}{n-1}}$$

where X_i 's are the sample observations, n is the sample size of data taken from process, and \bar{X} is the arithmetic average of the observations:

$$\bar{X} = \frac{\sum_{i=1}^n X_i}{n} .$$

This mean square root estimate of the standard deviation is recommended over the range estimate because the process capability study is usually an off-line study which intends to include all the inevitable variation sources.

C_p measure is good only for a process that can be adjusted to meet the target value. When the mean of the distribution is off the target, the measure is biased regardless of the values of the standard deviation.

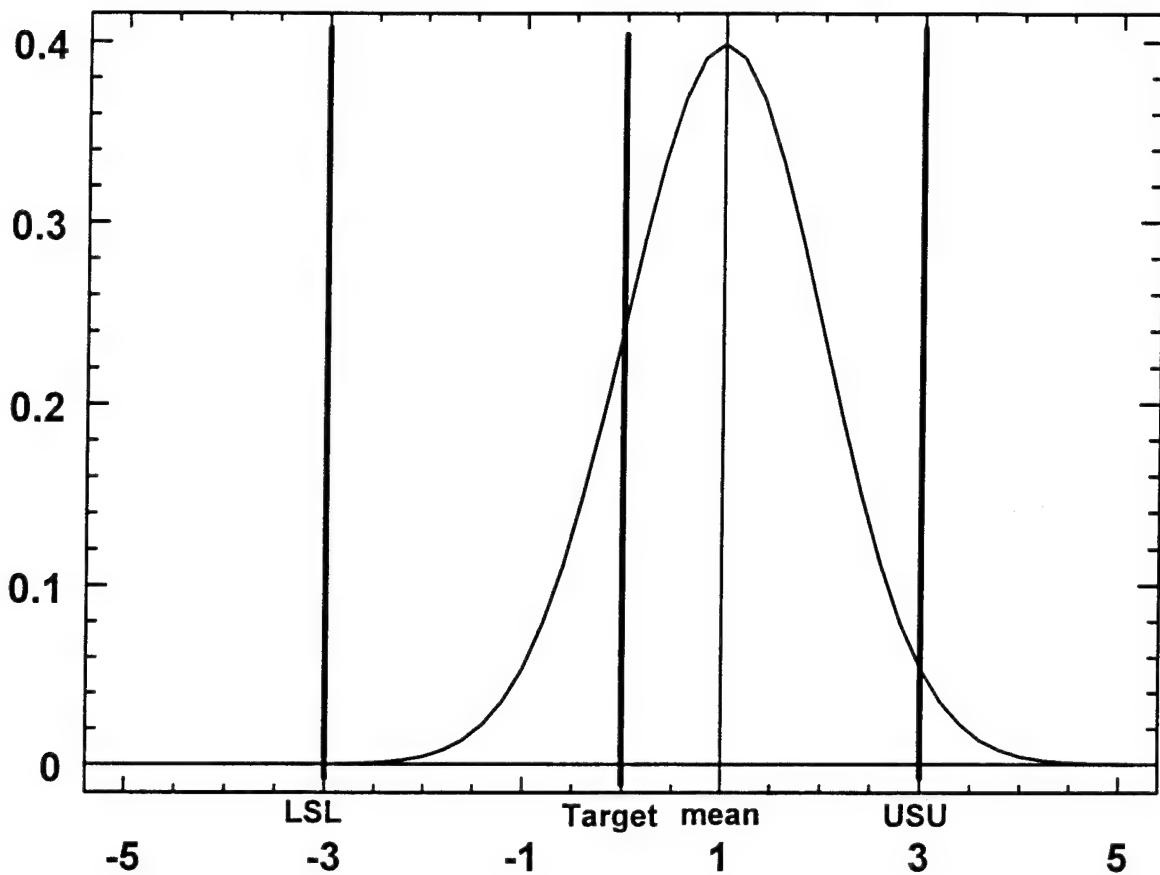


Figure 2: Process with a shifted mean

Figure 2 shows a process which has mean at 1 rather than at the target value 0. However, it still has a C_p value of 1.0. There is another concern with C_p measure. From the formula, it is clear that the C_p measure is suitable only for symmetric bilateral specification limits. Next, we should introduce a measure C_{pk} to resolve these problems regarding the C_p measure.

2.2 Process Capability Index for Asymmetric Processes C_{pk}

C_{pk} has the following form:

$$C_{pk} = \min[CPL, CPU] \text{ where}$$

$$CPU = \frac{USL - \mu}{3\sigma} \text{ and } CPL = \frac{\mu - LSL}{3\sigma}$$

To estimate C_{pk} , we again use the mean square estimate for the standard deviation and the arithmetic average for the mean:

$$\hat{C}_{pk} = \min[\hat{CPL}, \hat{CPU}], \text{ where}$$

$$\hat{CPU} = \frac{USL - \bar{X}}{3s} \text{ and } \hat{CPL} = \frac{\bar{X} - LSL}{3s}.$$

When the specification limits are symmetric against the target and the mean of the process coincides with the target and the value of C_{pk} coincides with the value of C_p . CPU and CPL can also be used for those characteristics with unilateral tolerance.

Though this measure solves the problems of asymmetric and unilateral specification tolerance it is however still inefficient for processes whose means are off target.

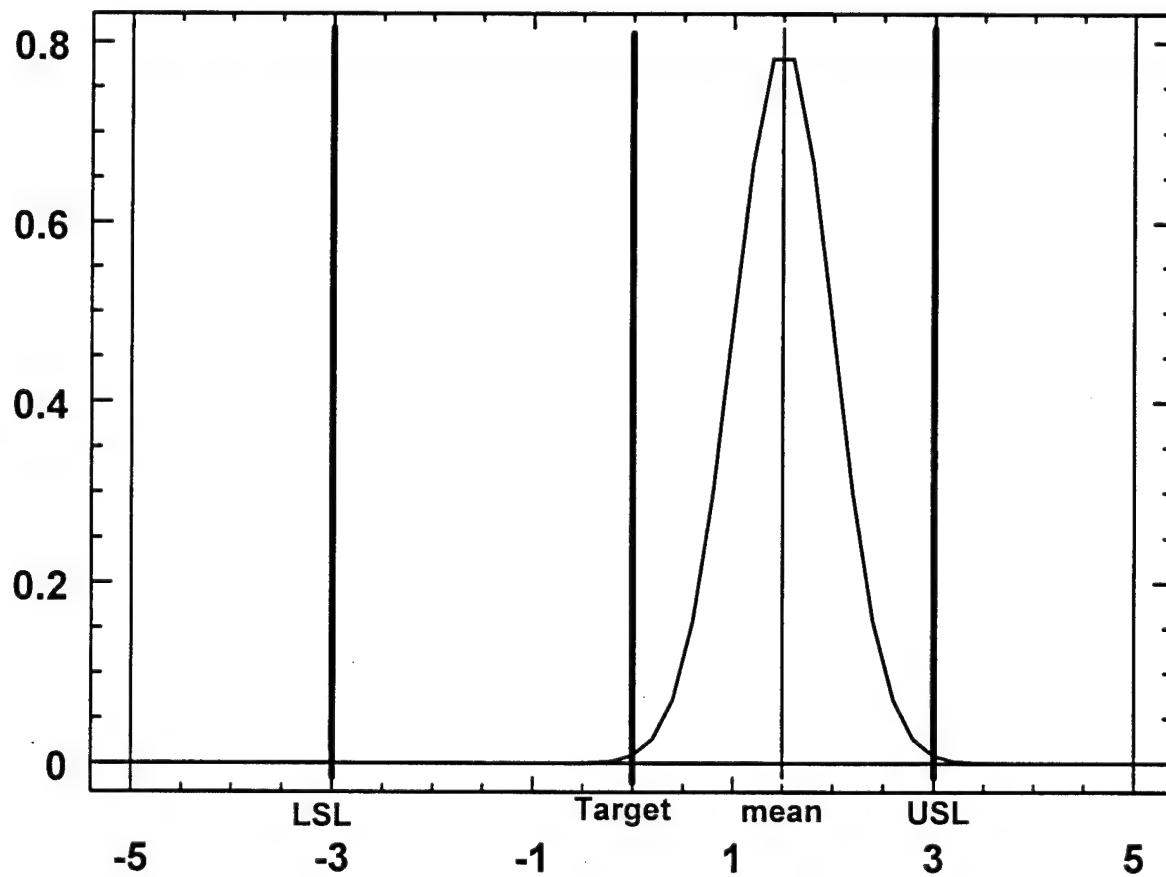


Figure 3: Process with a high C_{pk} and a shifted mean

The normal distribution shown in Figure 3 has mean of 1.5, which is well off the target 0, and a standard deviation of 0.5, so the C_{pk} is calculated as:

$$C_{pk} = \min\left[\frac{1.5 - (-3)}{3(0.5)}, \frac{3 - 1.5}{3(0.5)}\right] = 1.0$$

To take into account the off-target problem, we introduce C_{pm} measure.

2.3 Process Capability Index for Off-target Means C_{pm}

C_{pm} has the following form:

$$C_{pm} = \frac{USL - LSL}{6\sigma'}$$

where

$$\sigma' = \sqrt{E(X - T)^2}$$

is the square root of the mean square error against the target value. Since the mean square error can be further decomposed into two terms, variance and square deviation from target, σ' can be rewritten as:

$$\sigma' = \sqrt{\sigma^2 + (\mu - T)^2}$$

C_{pm} can be therefore written as:

$$C_{pm} = \frac{USL - LSL}{6\sqrt{\sigma^2 + (\mu - T)^2}} = \frac{C_p}{\sqrt{1 + \frac{(\mu - T)^2}{\sigma^2}}}$$

In other words, when the mean of the process coincides with the target value (T), then C_{pm} coincides with C_p . To estimate C_{pm} , we need first to estimate σ' :

$$\hat{\sigma}' = \sqrt{\frac{\sum_{i=1}^n (X_i - T)^2}{n}}$$

C_{pm} is then estimated:

$$\hat{C}_{pm} = \frac{USL - LSL}{6\hat{\sigma}'}$$

Like C_p , C_{pm} suffers from problems with asymmetric and unilateral tolerances. This measure is therefore further improved to the C_{pm}^* measure.

2.4 Generic Process Capability Index C_{pm}^*

C_{pm}^* has the following form:

$$C_{pm}^* = \frac{\min[USL - T, T - LSL]}{3\hat{\sigma}'}$$

This measure can be used for asymmetric bilateral tolerance. When the characteristic has only unilateral tolerance, the C_{pm}^* is calculated as:

$$C_{pm}^* = \frac{USL - T}{3\hat{\sigma}'} \text{ or } \frac{T - LSL}{3\hat{\sigma}'}$$

Again, this measure coincides with C_{pm} when the tolerance is symmetric bilateral and additionally with C_p when the mean coincides with the target. The estimate of C_{pm}^* is not different from the C_{pm} :

$$\hat{C}_{pm}^* = \frac{\min[USL - T, T - LSL]}{3\hat{\sigma}'}$$

where

$$\hat{\sigma}' = \sqrt{\frac{\sum_{i=1}^n (X_i - T)^2}{n}}$$

Finally, a comparison of the four PCI measures is presented in Appendix C.

3. Manufacturing Cost Estimate

To estimate the manufacturing cost, there are several major elements that should be taken into account: *production and schedule efficiency, raw materials, personnel, capital and equipment, and utility*. We now explain each element and the relationships among these elements to accurately estimate the final product unit.

- **Production Schedule/Efficiency**

A *minimum production capacity* should be determined based on a prior market study or logistic planning for the case of military supply. This production capacity requirement will lead to the determinations of *production rate* and *production shift schedule*. *Production rate* is the line production rate and *the production shift schedule* determines the operating time of the line to meet the required production capacity. *Process yield* and *efficiency* should then be addressed.

First, the production line should be broken down to element processes. Each process is then evaluated in terms of the process's efficiency. By *efficiency*, we mean the actual average production rate vs. the maximum (or projected) production rate. This is due to the fact that the process is often subject to operating problems such as breakdown and repair. After the process efficiencies are evaluated, it may be necessary to go back to replan production shift schedules in order to meet the minimum production capacity requirement.

Second, for each process, the production yield should be evaluated. By *yield*, we mean the percentage of products that are produced and meet quality requirements. For processes connected in series, the final production yield will be the multiplication of yields from individual processes. The production yield evaluations will be further demonstrated later in Sections 4.4 and 4.5. The results of the yield evaluations will be input into raw material cost estimate. Again, the yield evaluation may need to be fed back to readjust the production shift schedule. For *on-line quality inspection* systems, the *scraping* or *reworking* costs should be taken into account.

- **Raw Materials**

Raw materials include both ingredient materials and packaging materials. When considering the material cost per unit product, the following costs should be taken into account:

- 1) ingredient material purchase cost;
- 2) packaging material purchase cost;
- 3) scraping/reworking costs for yield less than 100%; and
- 4) material handling cost.

- **Personnel**

The personnel includes:

- 1) Administration personnel,
- 2) Operation supervisory,
- 3) Operation labors, and
- 4) Quality personnel.

The costs should be estimated for each category based upon the hours required from the planned production shift schedule.

- **Capital/Equipment**

Capital investments are as follows:

- 1) Production facility: administrative offices, plant floor and warehouse;
- 2) Production equipment: manufacturing, packaging and quality control equipment;
- 3) Contingency capital; and
- 4) Working capital.

The following costs should also be considered:

- 1) Maintenance/repair,
- 2) Equipment/facility depreciation,
- 3) Insurance,
- 4) Financing, and
- 5) Taxes.

- **Utility**

By *utility*, we mean the energy supplies required for the production/administration operations. These supplies may vary greatly depending on the type of productions. We list here some energy sources:

- 1) Natural gas,
- 2) Burning oil,
- 3) Process water,
- 4) Cooling water,
- 5) Steam,
- 6) Compressed air, and
- 7) Electricity.

If applicable, the following costs should be considered,:

- 1) Taxes,
- 2) Internal environmental costs: cleaning, facility erosion, and
- 3) External environmental costs.

We listed the main elements and costs considered under each element. It should be noted that the above listing serves as a guideline for manufacturing cost estimation but is certainly not the only elements that should be considered. Practitioners should develop their own manufacturing cost estimation scheme based on their own situations.

4. Producibility Index

We discussed the evaluations of process capability and manufacturing cost in previous sections. In this section, we propose a producibility index that includes these two evaluations as related to the newly designed product. We first present the index, then demonstrate step-by-step procedures that lead to the final calculated result of this index.

The producibility index (PI) proposed has the following form:

$$PI = [PCI_{critical}, PCI_{major}, PCI_{minor}, PCI_{average}, MC].$$

This index is in effect a vector index with 5 elements:

- $PCI_{critical}$: the minimum value of calculated PCI's for critical characteristics;
- PCI_{major} : the minimum value of calculated PCI's for major characteristics;
- PCI_{minor} : the minimum value of calculated PCI's for minor characteristics;
- $PCI_{average}$: the weighted geometric mean of PCI's for all quality characteristics; and
- MC : the manufacturing cost estimate.

Each of the five elements has its own irreplaceable evaluation towards the product's producibility. We will later elaborate on the classifications of the critical, major and minor quality characteristics. But in order to explain these five elements, let us keep in mind that these three types of characteristics represent quality characteristics with three different levels of importance. The process capability index (PCI) used here could be C_p , C_{pk} , C_{pm} , or C^{*pm} depending on the situation and the needs of study as discussed in Section 2. However, it should be noted that once an adequate index is chosen for a particular quality characteristic, the same index should be used throughout the calculations for the same characteristic. This is very important especially when conducting comparative producibility studies for different product and process designs.

As indicated above, the first three elements are the minimum PCI's from three types of quality characteristics. It is important to know the minimum PCI value for each type of characteristics because an unsatisfactorily low PCI value for even just one quality characteristic will result in the dismissal of the product and process design regardless of the high overall average of the PCI. As explained in Section 2, a value of PCI greater than one is essential for any production setting with statistical process control (SPC) charts. A PCI value less than one

indicates that the window of the control limits is wider than the specification tolerance and therefore violates the control chart's role as a precaution warning device.

The weighted geometric mean of all PCI's is an index of the overall process performance in producing the designed product. Three different types of quality characteristics and different production rates should be weighted differently to reflect the relative importance of the characteristics and the production capacity requirement. The geometric mean is chosen here to calculate the overall average because of its two desirable properties:

- 1) The geometric mean is more sensitive than the arithmetic mean to small values. This is desirable because a smaller PCI value diminishes producibility considerably.
- 2) A value of zero will result in a zero geometric mean regardless of how high other values are. This is also desirable since a process with PCI value of zero for any one characteristic is considered absolutely unacceptable regardless of the quality level of other characteristics.

The manufacturing cost (MC) estimate should follow procedures described in Section 3. This cost estimate is an important reference of the product's producibility because it represents the actual manufacturing cost. It should not, however, be treated as the only reference for a product's producibility since there could exist some processes that have a very low manufacturing cost but perform poorly in producing *constant* quality products. It should be noted that the only quality concern of the product and process design included in the manufacturing cost estimate is the production yield. As discussed in Section 3, the production yield is not enough to represent the process performance with regard to product quality. On the other hand, the process capability index alone cannot dictate the producibility because the production could be unnecessarily costly.

We have provided the rationales behind the proposed producibility index. We now describe the step-by-step procedures to carry out the calculation of the producibility index. The calculation steps are as follows:

- 1) Define Quality Characteristics and Production Capacity Requirement;
- 2) Identify the type of PCI to be used;
- 3) Determine the rational subgroup and sampling methodology;
- 4) Sample data and calculate PCI values;

- 5) Calculate production yield for manufacturing cost estimate; and
- 6) Calculate producibility index.

4.1 Quality Characterization and Production Capacity Requirement

The first step in evaluating the producibility is to define the characteristics as related to the product's functionality and safety requirements. These characteristics also define a product's individuality. From the principles of DFM and concurrent engineering, the following steps are required for defining a product:

- 1) Interact with marketing sales and manufacturing engineering to recognize the needs of customers and manufacturing constraints;
- 2) Specify performance and safety requirements to meet needs from 1;
- 3) Investigate the feasibility of the specified performance requirements from 2. Go back to 1 if necessary;
- 4) Generate ideas and solutions regarding the feasible requirements from 3; and
- 5) Develop a product prototype in cooperation with manufacturing and production engineers.

After going through the above steps, a new product design is now well defined with a set of product characteristics and a minimum requirement for the production capacity. For the purpose of evaluating producibility, the product characteristics should be further identified in terms of the following properties:

- **Importance**

As mentioned earlier, the characteristics defined may have different levels of importance with regard to the product's functionality and safety features. To evaluate the producibility, the characteristics should be weighted differently according to their levels of importance. In our approach, we classify the defined characteristics into the following three categories of importance level:

Critical: Those characteristics that could cause damages to human, environment, or any unrecoverable damages when the corresponding specifications are violated.

Major: Those characteristics that cause the product malfunctioning, but do not cause damages as critical characteristics do, when the corresponding specifications are violated.

Minor: Those characteristics that diminish the product's usability, while they do not cause damages and malfunctioning as critical and major characteristics do, when the corresponding specifications are not met.

Each characteristic defined should be assigned to one of the three categories, which are mutually exclusive. This assignment will later affect the weight of the characteristic in the evaluation of the overall process capability average.

- **Variable/Attribute**

The characteristic is either a *variable* that can be expressed numerically or an *attribute* that can only be described qualitatively, as either defective or non-defective.

- **Stationary Characteristics**

A defined characteristic should also be differentiated by its stationary nature. A *stationary* characteristic is the characteristic that has a process *mean* (for the variable characteristics), or *yield* (for attribute characteristics) that is likely to remain constant throughout the long-term production runs. Characteristics that behave otherwise are called *nonstationary* characteristics.

Such behavior of product characteristic will affect the calculation procedures of PCI's and should be clearly identified before sampling data.

- **Tolerances**

There are different types of specification limits (tolerances) for the characteristics. First, there are *bilateral* tolerances with both upper and lower specification limits. Second, there are *unilateral* tolerances with only an upper or a lower specification limit. For the bilateral tolerance, there is a *symmetric* type of tolerance where the target is at the center between the upper and lower limits and there is an *asymmetric* type of tolerance where the target is not at the center.

This type of the tolerance can be easily observed and identified for *variable* types of characteristics. For the *attribute* type of characteristics, most characteristics are unilateral, that is, they are either defective or non-defective. However, there may exist an attribute characteristic that has two-way possibilities of defects. This case may be considered as a bilateral tolerance.

4.2 Type of PCI to be used

Due to the different properties of the characteristics, it is necessary to choose different types of PCI to reflect the true process performance of the characteristics. Different types of PCI's have been discussed in Section 2. Here, we list the type of characteristics and the corresponding PCI to be used.

- variable/stationary/bilateral/symmetric: C_p
- variable/stationary/bilateral/asymmetric: C_{pk}
- variable/stationary/unilateral: C_{pk}
- variable/nonstationary/bilateral/symmetric: C_{pm} (or C_p for long-term production study)
- variable/nonstationary/bilateral/asymmetric: C_{pm}^* (or C_{pk} for long-term production study)
- variable/nonstationary/unilateral: C_{pm}^* (or C_{pk} for long-term production study)
- attribute/stationary/bilateral: C_p (converted from short-term production yield)
- attribute/stationary/unilateral: C_{pk} (converted from short-term production yield)
- attribute/nonstationary/bilateral: C_p (converted from long-term production yield)
- attribute/nonstationary/unilateral: C_{pk} (converted from long-term production yield)

4.3 Rational Subgrouping and Sampling Methodology

The objective of the rational subgrouping is to adequately exclude and include the sources of randomness for a specific purpose of variability study. The purpose of this project is to study the process capability as related to a new product design. Therefore, we would like to know how the product quality varies when the product is actually produced. To calculate the process capability indices, we need to estimate the standard deviation as a measure representing the quality variation and then compare it with the specification limits. By doing this (see Section 2), we will be able to evaluate the process performance against the projected product specifications. There are many sources of variation present in the actual production process. Though some are avoidable others are considered unavoidable. For the purpose of the producibility study, we need to subgroup the data sample from the process such that the unavoidable variability sources are included and those avoidable are excluded when estimating the standard deviation. For example, deviations due to raw material quality may be unavoidable and should be included in the study. In other times, the raw material deviations can be well compensated by applying some control measures. In this case, this type of variation source should be excluded. Varying production rate also appears to be an important source of variation and is often unavoidable. For example, if we produce units at high production rate, we may increase variability in the product characteristics and vice versa. Therefore, different sample data may need to be taken to reflect the "true" overall process capability instead of just a process capability for a specific production rate. The effect of varying the production rate is further discussed later in the calculation of the average process capability index.

Rational subgrouping is a very important step in the process capability study. An inadequate subgrouping sample will cause a severe bias in the estimation of the standard deviation and the process capability indices. To prevent biasness of the estimates, design and production engineers together should carefully plan the sampling scheme. Though the scheme often varies for different situations, we provide some generic guidelines as a reference for practitioners.

1. Clearly state the objectives of the data collection.
2. Deliberate as detailed as possible the actual process where data sample to be taken from.
3. List the possible sources of variation.
4. Determine rational subgroups to exclude and include appropriate variation sources.
5. Determine time interval for rational subgroups sampling to avoid dependency between groups.

4.4 PCI calculations

In Section 2, we have discussed the formulas for various process capability indices. We now provide procedures for the calculations of the PCI for each type of product characteristics.

- **variable/stationary/bilateral/symmetric:**

This type of characteristic has the most straightforward procedures for the calculation of the PCI. We now demonstrate the step-by-step procedures of estimating PCI. First, we consider the case when the characteristic is variable; that is, it can be expressed numerically. The mean square root estimate of the standard deviation shown in Section 2 can be therefore applied here; that is,

$$\hat{\sigma} = \sqrt{\frac{\sum_{i=1}^n (X_i - \bar{X})^2}{n-1}}$$

Second, the characteristic is stationary; that is, the mean of the product characteristic remains constant throughout the "in-control" state of the production process. With this constant mean, one can always preset the process such that the mean coincides with the projected target value. This means that we can evaluate the process capability without considering the mean deviations from the target.

Third, the characteristic has a bilateral, symmetric tolerance; that is, the target is in the center of the specification limits. This implies that a simple C_p can be used. To calculate C_p , one needs: the specification width (USL-LSL) and the standard deviation as shown in Section 2.1. Hence, the PCI is calculated as:

$$PCI = \frac{USL - LSL}{6\hat{\sigma}}$$

- **variable/stationary/bilateral/asymmetric:**

This type of characteristics is essentially the same as the preceding type except that the bilateral tolerance is asymmetric. The first two properties ensure that the mean square root estimate of the standard deviation can be used; and concerns about mean deviations from the target can be dismissed. As discussed earlier, when the tolerances are asymmetric the C_{pk} should be used instead of C_p and take the minimum between the two capability indices calculated against the upper specification limit and the lower specification limit is chosen as the C_{pk} value. Since the tolerance is known to be asymmetric, the target value (T) must be known in addition to USL LSL. The PCI can then be calculated as:

$$PCI = \min\left[\frac{USL - T}{3\hat{\sigma}}, \frac{T - LSL}{3\hat{\sigma}}\right],$$

where μ (mean) is replaced with T (target value) since the stationary property allows the mean to be set at the target value and remains constant.

- **variable/stationary/unilateral:**

When the target value (T) is known, the PCI should be calculated using C_{pk} as follows:

$$PCI = \frac{USL - T}{3\hat{\sigma}} \text{ or } \frac{T - LSL}{3\hat{\sigma}},$$

where the mean is again replaced with T (target value) because of the stationary property.

It should be noted that this type of characteristics also includes the-bigger-the-better and the-smaller-the-better types of characteristics. In these cases, the C_{pk} is calculated as:

$$PCI = \frac{USL - \hat{\mu}}{3\hat{\sigma}} \text{ or } \frac{\hat{\mu} - LSL}{3\hat{\sigma}},$$

where the sample mean ($\hat{\mu} = \bar{X} = \sum X_i / n$) should be set, within the process capability, as large or as small as possible for the-bigger-the-better or the-smaller-the-better types of characteristics, respectively.

- **variable/nonstationary/bilateral/symmetric:**

When the characteristic is nonstationary, it implies that the mean of the characteristic of concern is quite sensitive to various sources of variations. This means that we should consider the possible mean deviations from the target when studying the process capability. The appropriate PCI that includes the mean deviations is C_{pm} . To calculate the C_{pm} , an associated target value should be clearly defined. The PCI is calculated as:

$$PCI = \frac{USL - LSL}{6\sqrt{\frac{\sum_{i=1}^n (X_i - T)^2}{n}}}$$

For most processes, the overall mean for the long-term production run can be still set at the target value despite the nonstationarity of the short-term mean. Therefore, when a target value is not yet determined, the study should be conducted for a long-term production run to include various mean deviations and the C_p can then be used instead of C_{pm} . This is because the mean square root estimate of the standard deviation takes into account the possible mean deviations from the target when the long-term mean can be set at the target value.

- **variable/nonstationary/bilateral/asymmetric:**

When the variable characteristic is nonstationary with asymmetric bilateral tolerance, then C_{pm}^* is the appropriate measure. That is,

$$PCI = \frac{\min[USL - T, T - LSL]}{3\sqrt{\frac{\sum_{i=1}^n (X_i - T)^2}{n}}}.$$

Like the previous type of characteristics where the bilateral tolerance is symmetric, a C_{pk} from a long-term production study can be used and set as the target value.

- **variable/nonstationary/unilateral:**

When the nonstationary variable characteristic is unilateral with a known target value, the C_{pm}^* is used as follows:

$$PCI = \frac{USL - T}{3\sqrt{\frac{\sum (X_i - T)^2}{n}}} \text{ or } \frac{T - LSL}{3\sqrt{\frac{\sum (X_i - T)^2}{n}}}$$

Again, when the target value is not yet determined, C_{pk} can be used instead by substituting T with the mean of the process obtained from a long-term production run.

For the-bigger-the-better and the-smaller-the-better type of characteristics, the process should be tested with its highest possible capability for a long-term production run and C_{pk} is calculated as follows:

$$PCI = \frac{USL - \hat{\mu}}{3\hat{\sigma}} \text{ or } \frac{\hat{\mu} - LSL}{3\hat{\sigma}}$$

- **attribute/stationary/bilateral:**

The attribute characteristics have very different calculation procedures from that of the variable characteristics since they only have qualitative measures instead of numerical measures; that is, the measure is either "conforming" or "nonconforming" to the specification. Moreover, there is no numerical upper or lower specification limits. Thus, the PCI formulas are not applicable for attribute type of characteristics. However, instead of calculating the PCI directly, we can first estimate the percentage yield of conforming products and then convert it to a PCI value by assuming an underlying normal distribution.

To estimate the yield, we usually use a measure called Parts Per Million (ppm) which represents number of nonconforming parts per million of produced parts. This measure is used due to the fact that a capable process usually requires the production of hundreds of thousands or even millions of parts before a nonconforming part is produced. To obtain an estimated ppm, engineers need to run the production and stop only when a projected number of nonconforming parts has been produced.

As mentioned, a capable process may require millions of parts to produce just one defective part. In order to preserve resources, engineers can choose to stop the production when only one nonconforming part is produced. However, if preservation of resource is not of concern, the process should be run until at least 3 nonconforming parts are found in order to obtain a more reliable estimate of ppm especially for nonstationary production processes.

The probability distribution for r nonconforming parts in a total of N parts produced with a probability p of nonconformance is usually assumed to be a Poisson; that is:

$$\Pr(r|N, p) = \frac{(Np)^r e^{-Np}}{r!}$$

The Poisson distribution is a limiting distribution of a binomial distribution with a very large number, N , of trials (produced parts for our discussion) and a very small probability, p , of occurrence (probability of a nonconforming parts in our discussion). Based on the underlying Poisson distribution, we can then estimate the average ppm given a number of N parts produced with r nonconforming parts:

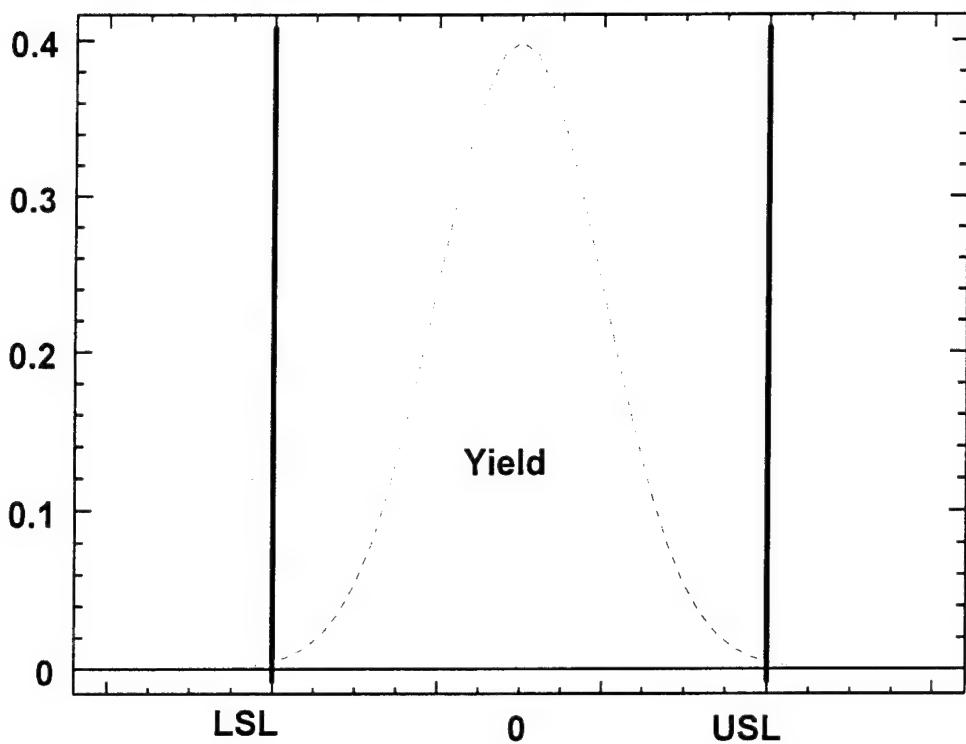
$$\hat{ppm} = \frac{\chi^2_{(0.5, 2r)}}{2N} 10^6$$

where $\chi^2_{(0.5, 2r)}$ is the value below which the chi-square distribution with $2r$ degrees of freedom has a probability of 0.5. The above estimate is the "best ppm estimate" in terms of its stability given a small number (≤ 10) of defective products is found. A table listing the estimated ppm for various values of N and r (≤ 10) is provided in Appendix A. For $r > 10$, the following simple estimate is satisfactory:

$$\hat{ppm} = \frac{r}{N} 10^6$$

After the yield (in terms of ppm) is estimated, one can assume an imaginary numerical measure scale with specification limits for this attribute characteristic. Assuming also a normal distribution for the characteristic's imaginary variable, we can now convert the yield to a PCI value. Here, the attribute characteristic has two-way possibility of nonconformance (bilateral). We can thus have the following imaginary normal distribution with mean 0 and standard deviation 1:

Prob. Density Fcn. and Specs Tolerance



where

$$Yield = 1 - \frac{ppm}{10^6} = 1 - 2\Psi(USL)$$

and

$$\Psi(x) = \int_x^\infty \frac{1}{\sqrt{2\pi}} e^{-u^2/2} du$$

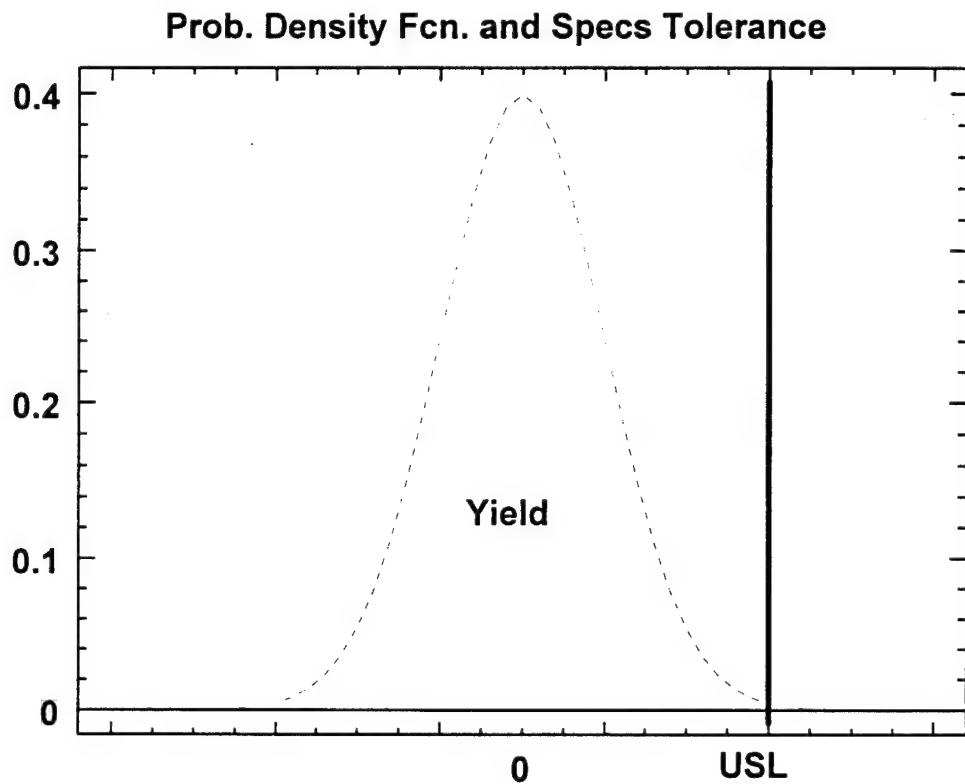
is the probability for having value of x and beyond. From these relationships, the USL can be found from standard table (such as Appendix B) and a PCI is then calculated as:

$$PCI = \frac{USL - 0}{3\sigma} = \frac{USL}{3},$$

where σ is 1 for the standard normal distribution.

- attribute/stationary/unilateral:

This stationary attribute characteristic has unilateral nonconformance. As in the previous case, we should first run the production to obtain some nonconforming parts. A ppm measure is then estimated based on the underlying Poisson assumption. A numerical normal distribution is then assumed to convert the ppm measure to the corresponding PCI measure. However, in the unilateral case we have only one imaginary specification limit:



where

$$Yield = 1 - \frac{ppm}{10^6} = 1 - \Psi(USL).$$

Again, the USL can be found from the standard table for $\Psi(\cdot)$ (see Appendix B). The PCI is now evaluated:

$$PCI = \frac{USL - 0}{3\sigma} = \frac{USL}{3}.$$

where σ is 1 for the standard normal distribution.

The following table provides some basic PCI values and their corresponding process yields. (Other values can be calculated from the above formulas and the table in Appendix B.)

PCI values	Yield (unilateral spec.)	Yield (bilateral & symmetric spec.)
0.9	0.996533	0.993066
1.0	0.998650	0.997300
1.1	0.9995165	0.999033
1.2	0.9998408	0.9996816
1.3	0.99995178	0.99990356
1.4	0.99998656	0.99997312
1.5	0.999996549	0.999993098
1.6	0.999999181	0.999998363
1.8	0.999999963	0.999999926
2.0	0.999999998	0.999999997

- **attribute/nonstationary/bilateral or unilateral:**

For the nonstationary attribute characteristics, the procedures for calculating ppm and PCI are essentially the same as those for the stationary case except that much more units are required to be produced in order to obtain a more reliable estimate of the ppm.

4.5 Manufacturing cost estimate:

The manufacturing cost estimate has been discussed in Section 3. In this section, we demonstrate how the production yield can be obtained in order to accurately estimate the manufacturing cost. There are two basic components for estimating the production yield: *quality yield* and *production loss*. *Quality yield* is the percentage of products, that meet all product specifications, produced under normal production condition. *Production loss* is the product percentage that is usually lost during the production run due to the production start-up, change-over or any other causes. The production loss should be estimated based on information from

pilot production runs or from other similar types of productions when the process design is currently not feasible or is not ready for a formal production run.

We first discuss the calculations for the quality yield. For the attribute characteristics, the yield of the process is estimated from the ppm measure as:

$$\text{Quality Yield} = 1 - \frac{\text{ppm}}{10^6}.$$

For the variable characteristics, we need to transform the specification limits to the corresponding limits for the standard normal distribution:

$$LSL' = \frac{LSL - \hat{\mu}}{\hat{\sigma}} \text{ and } USL' = \frac{USL - \hat{\mu}}{\hat{\sigma}}.$$

where LSL' and USL' are the limits obtained from the standard normal distribution that correspond the LSL and USL of the quality characteristic respectively. The quality yield is now established:

$$\text{Quality Yield} = \Psi(LSL') - \Psi(USL')$$

for bilateral tolerance and

$$\text{Quality Yield} = \Psi(LSL') \text{ or } 1 - \Psi(USL')$$

for unilateral tolerance. Appendix B can be again used to find the $\Psi(\cdot)$ values. After estimating the quality yield and the production loss (as defined earlier), we calculate the production yield as:

$$\text{Production Yield} = (1 - \text{Production Loss}) \times \text{Quality Yield}$$

4.6 Producibility Index Calculation:

As stated at the beginning of this section, the proposed producibility index is expressed as:

$$PI = [PCI_{crit_min}, PCI_{major}, PCI_{minor}, PCI_{average}, MC]$$

Suppose now that we have a total of n characteristics of the product. Further, assume that among the n characteristics, n_1 of them are critical; n_2 are major; and n_3 are minor. That is,

- critical characteristics: X_1, X_2, \dots, X_{n_1} ;
- major characteristics: Y_1, Y_2, \dots, Y_{n_2} ;
- minor characteristics: Z_1, Z_2, \dots, Z_{n_3} ; and
- $n = n_1 + n_2 + n_3$.

The PCI for each characteristics is calculated by following the procedure described in Section 4.3. We then calculate:

$$PCI_{critical} = \min[PCI_{X_1}, PCI_{X_2}, \dots, PCI_{X_{n_1}}],$$

$$PCI_{major} = \min[PCI_{Y_1}, PCI_{Y_2}, \dots, PCI_{Y_{n_2}}] \text{ and}$$

$$PCI_{minor} = \min[PCI_{Z_1}, PCI_{Z_2}, \dots, PCI_{Z_{n_3}}].$$

To calculate the weighted geometric mean of PCI values for all characteristics, we need to assign weights to each type of characteristics (Derringer (1994)). We use ideal weights w_1 : w_2 : w_3 to represent the weight ratio for critical, major and minor characteristics, respectively. The weight ratio can be assigned by practitioners based on their needs and situations. We, however, suggest a ratio of 5:3:1. The weighted geometric mean is calculated as:

$$\begin{aligned} PCI_{average} &= [(PCI_{X_1} \dots PCI_{X_{n_1}})^{1/n_1}]^{\frac{w_1}{\sum w_i}} [(PCI_{Y_1} \dots PCI_{Y_{n_2}})^{1/n_2}]^{\frac{w_2}{\sum w_i}} [(PCI_{Z_1} \dots PCI_{Z_{n_3}})^{1/n_3}]^{\frac{w_3}{\sum w_i}} \\ &= (PCI_{X_1} \dots PCI_{X_{n_1}})^{\frac{w_1}{n_1 \sum w_i}} (PCI_{Y_1} \dots PCI_{Y_{n_2}})^{\frac{w_2}{n_2 \sum w_i}} (PCI_{Z_1} \dots PCI_{Z_{n_3}})^{\frac{w_3}{n_3 \sum w_i}} \end{aligned}$$

The calculation above is based on the assumption that the individual PCI's do not vary with the production rates. Now, suppose the process performance is sensitive to the production rate for some of the product characteristics. In this case, we need to refine the calculations for the individual PCIs in order to reflect the effect of production rate on the process capability.

Assume that the projected production rate is PR and the tested process mainly has three levels of production rates: low, medium, high or PR_l , PR_m , PR_h . We propose using weighted geometric mean of the PCI for the characteristic which is sensitive to the production rates with a weight ratio of:

$$w_l:w_m:w_h = \frac{PR_l}{PR} : \frac{PR_m}{PR} : \frac{PR_h}{PR}$$

Let PCI_l , PCI_m , and PCI_h be the PCI values calculated for low, medium and high production rates, respectively. The average PCI for the characteristic is then calculated as:

$$PCI = (PCI_l)^{\frac{w_l}{w_l+w_m+w_h}} (PCI_m)^{\frac{w_m}{w_l+w_m+w_h}} (PCI_h)^{\frac{w_h}{w_l+w_m+w_h}}.$$

This PCI is then used for calculating the overall average PCI as discussed earlier.

To estimate the production rate, we need an overall production yield that takes into account all characteristics of concern:

$$Yield = Yield_{X_1} \bullet \dots \bullet Yield_{X_{n_1}} \bullet Yield_{Y_1} \bullet \dots \bullet Yield_{Y_{n_2}} \bullet Yield_{Z_1} \bullet \dots \bullet Yield_{Z_{n_3}}.$$

We conservatively assume that all characteristics are independent and therefore calculate the final yield of the quality products by multiplying the yields for individual characteristics. After the yield is estimated the manufacturing cost can then be calculated as discussed in Section 3.

We have calculated all the elements of the producibility index (PI) vector. The PI calculated for a specific product/process design is then compared to the PIs of other alternative designs' PIs. The best design based on the PI comparison is then chosen for the actual production.

5. Examples of Producibility Indices

In this section, we use the processes designed for producing Meal-Ready-to-Eat (MRE) pouches as examples to demonstrate the proposed producibility index. The quality specifications of MRE pouches have been specified in a series of military standard documents. Here, we are

particularly interested in two products: beef stew and ham slice in MRE pouches (please refer to MIL-B-44059C and MIL-H-44063D, respectively). For the first product, we first test different pouch forming designs where different pouch materials and forming pressures are used. Second, we study effects of different target fill weight designs on the producibility index. For the second product, we compare two different methods of slicing ham into the desired dimensions. We also compare the performance of using a robot or human in placing the ham slices into the open pouches. Comparisons are conducted based on the producibility index proposed above. The calculations of the producibility indices are performed using a spreadsheet program that is specifically designed for the MRE production processes.

5.1 Process/Product Designs for the Beef Stew MRE Pouches

The products produced in this study are beef stew pouches. The beef stew is prepared off-line and placed in a filler. Pouches are first formed by applying pressure on the *bottom* film. These formed pouches are then filled with the beef stew using a filler called Raque Filler. Finally, the filled pouches are sealed with a *top* film which is made of the same material as that of the bottom film. The forming, filling and sealing processes handle six pouches simultaneously per cycle. We now study the effects of different designs on the pouch manufacturing cost and the pouch integrity and quality.

In the study, we first focus on the design of the forming process. There are two variables that we try to manipulate: the pouch material and the forming pressure. Both variables dictate the depth, and consequently the volume, of the pouch. For the pouch material, we use two different films produced by Reynolds and Aluswiss. For the forming pressure, we choose two settings for each pouch material. The major concern in this study is the pouch quality that includes critical defects such as unsatisfactory seal width, seal wrinkles, tear/cuts/holes and delamination on the pouch surface. In order to prevent contamination on the edges of opened pouches, and consequently the seal integrity of the finished pouches, due to accidental splashes by the filling process, the speed of the filling process should be adjusted according to the smaller volume of the formed pouch. The larger the pouch volume, the easier, and thus faster, the filling process. On the other hand, the larger pouch volume requires higher forming pressure applied on the bottom film. This higher pressure may result in causing surface defects on the pouch such as delamination and tears. The higher pressure also may cause blowout of the bottom film and thus decreases the efficiency of the entire forming/sealing process due to the stopping of the production line and purging the blown-out pouches before resuming production.

Secondly, we study the effects of different designs on the target fill weights. According to the military standards (MIL-B-44059C), there are minimum requirements for both the net weight and the drained weight of the finished product. When the target fill weights are increased, the process capability against the minimum requirements increases. However, this will result in an increase of the manufacturing cost. It is obvious that there is a tradeoff between the process capability and the manufacturing cost as the target fill weight increases. The producibility index is particularly designed to present the tradeoff and to provide information for decision making on the process/product designs.

We will first analyze the effects of different pouch forming designs on the manufacturing cost given the advantages and disadvantages described above. Following the cost analysis, we study at the process capability index regarding the pouch quality. Through comparisons of both the cost and the process capability, we choose the best design and calculate the producibility index for this design. We then demonstrate the use of the producibility index in the comparison of different target fill weight designs.

5.1.1 Manufacturing Cost Analysis for Pouch Forming Designs

The elements of the manufacturing cost analysis have been presented in Section 3. Appendix D presents a complete spreadsheet program that details the elements and the corresponding numbers. In Appendix E, we have a visual representation and formulas of this cost analysis model. We present only the changes in the elements of cost analysis resulting from different designs in the forming process. The settings for each design are shown in the following table.

Design	Pouch Film	Forming Pressure	Open Pouch Volume
A	Reynolds	18 psi	260 cc
B	Reynolds	22 psi	320 cc
C	Aluswiss	27 psi	330 cc
D	Aluswiss	24 psi	305 cc

Each combination of the film type and the forming pressure results in a different pouch volume. As discussed earlier, the greater the volume, the faster the filling speed. On the other hand, the greater the forming pressure, the less efficient the pouch forming process due to possible blowout of the bottom film. The blowout of the bottom film will also increase the loss

of the film material and thus decrease the actual yield of the pouch material used in the production. In the following table, we present the effects of each design on some basic elements for the manufacturing cost analysis.

Design	Filling Speed*	Forming Process Efficiency*	Pouch Material Yield*	First Inspection Yield	Final Inspection Yield**
A	60	90%	98%	88.5%	83%
B	96	85%	95%	77%	93.8%
C	102	80%	90%	92.3%	100%
D	87	90%	98%	84.9%	100%

In Design A, the minimal formed pouch (260 cc) requires a slow filling speed to avoid seal contamination. Because of the slow speed, the line efficiency and pouch material yield for Design A are relatively high. In Design B, the pouch is formed to the maximum limit (320 cc) for the pouch film from Reynolds. As a result, the line speed can be higher than that in Design A but line efficiency and pouch yield are lower due to occasional blowouts. Design C has the largest formed pouch (330 cc) which enables the line to run in a maximum speed. The line efficiency and pouch yield are, however, the lowest due to a larger number of blowouts. In Design D, the same pouch film (Aluswiss) as in Design C is used but the lesser formed pouch (305 cc) results in better pouch yield and line efficiency but lower line speed.

For all designs, the pouches produced after the forming/sealing process are subject to two 100% visual inspections. The first is performed immediately after the pouch forming/sealing process to sort out defective pouches that fail to meet specifications on the pouch seal and the surface qualities due to poor film qualities or improper sealing process and material handling. The second inspection is performed after the sterilization retort process, the pouches are 100% visually inspected again to sort out defective pouches due to damages on the pouch surface during retort process and handling (loading and unloading) of pouches before and after the retort process. The yields resulting from these two 100% inspections are both listed in the above table and are based on actual observations. Both inspections will greatly affect the final manufacturing

* The numbers are based on expert opinions not actual experimental data.

** The final inspection did not include pouch discoloration a defect. The current manufacturer of the MRE film is still working on resolving this issue.

cost. In Appendix D, we describe in detail all the elements given in Section 3 focusing only on Design C. The following table shows the manufacturing cost calculated using the cost analysis model described in Appendices D and E.

Design	Manufacturing Cost per Pouch
A	\$1.573
B	\$1.370
C	\$1.184
D	\$1.231

5.1.2 Process Capability Study for the Pouch Defects

The quality of the pouch surface and seal is the only quality characteristic of concern after the pouch forming process. The pouch defects include insufficient seal width ($\leq 1/16$ inch), seal wrinkles, pouch inclusions, delamination, and tears/cuts/holes (please refer to MIL-P-44073B). When any of the above defects is found, the pouch is considered defective and cannot be used. Thus, this characteristic is considered a *critical attribute* quality characteristic and is also *stationary*. Moreover, the quality characteristic is considered *unilateral* since the defects described above are all one-directional. Now, assume that the two 100% visual inspections are 99% effective; that is, among 100 defective pouches, 99 of them will be sorted out through these two inspection procedures. Based on this assumption, we calculate the number of defective pouches per 100 pouches after the two 100% inspections:

$$\text{Defective Level (\%)} = \left(\frac{1}{Yield_{first} \times Yield_{final}} - 1 \right) \left(\frac{1}{Inspection\ Efficiency} - 1 \right) \times 100\%$$

where $Yield_{first}$ is the yield from the first 100% inspection; $Yield_{final}$ is the yield from the final 100% inspection; and *Inspection Efficiency* is defined as:

$$\text{Inspection Efficiency} = \frac{\text{number of defective pouches discovered}}{\text{total number of defective pouches}}.$$

An imaginary standard normal distribution with an upper specification limit is then established as discussed earlier:

$$\Psi(USL) = \frac{\text{Defective Level} (\%)}{100}.$$

Since this quality characteristic is considered unilateral, the *PCI* can then be calculated as:

$$PCI = \frac{USL}{3}.$$

The results from the experiments are shown in the following table:

Design #	Yield _{first}	Yield _{final}	Inspection Efficiency %	Defective Level %	PCI
A	0.885	0.83	99%	0.365%	0.8943
B	0.77	0.938	99%	0.388%	0.8875
C	0.923	1	99%	0.0843%	1.0469
D	0.849	1	99%	0.1796%	0.9707

It should be mentioned that the defective level is not estimated using the "best ppm estimate" presented earlier because there are more than 10 defective pouches found in each experiment design.

We now compare the PI values for different process/product designs as shown below:

Design	PI
	<i>[PCI_{critical}, PCI_{major}, PCI_{minor}, PCI_{average}, MC]</i>
A	[0.8943, -, -, 0.8943, 1.573]
B	[0.8875, -, -, 0.8875, 1.370]
C	[1.0469, -, -, 1.0469, 1.184]
D	[0.9707, -, -, 0.9707, 1.231]

From the above comparison, Design C is an obvious choice given its superior PCI and lower manufacturing cost. It should be noted that there are other quality characteristics that are specified in the military standard but not taken into account in the comparison because they are not affected by the process/product design addressed here.

Examining only the quality characteristic of pouch defects, the process appears incapable even for the best design D. The consumer, military in this case, usually imposes a very strict acceptance sampling plan for the critical quality characteristic. In the military standard (MIL-P44073B), a sample of 200 pouches are taken from a finished product lot. The lot is only accepted when all 200 pouches are found nondefective. Assuming Poisson probability distribution, we can estimate the probability of acceptance (P_a) of the lot in terms of the sampling plan and the actual defective level in a lot (p):

$$P_a = \sum_{i=0}^c \frac{e^{-np} (np)^i}{i!}$$

where n is the sample size and c is the criterion such that when the number of defects exceeds c , the lot is rejected. In the case of pouch defects, n is 200 and c is 0. In Appendix H, we present the Operating Characteristic (OC) curve for this sample plan and a table that shows various actual defective levels and their corresponding expected acceptance probability. From the table, one can find that to have 98% of the finished product lots to be accepted, the actual defective level should be less than 0.0001, that is, a yield of 0.9999. If we translate the yield to a PCI value, the PCI value should be no less than 1.24 in order to have 98% of your finished products accepted.

In our process design (C), the yield is merely 0.9157 (PCI=1.0469). This means that the acceptance rate (from Appendix H) will be only about 85%. This is certainly not satisfactory and the process should be further improved.

In the next section, we study the tradeoff between the manufacturing cost and the process capability for different designs of the target fill weights.

5.1.3 Producibility Indices for Different Designs of the Target Fill Weights

In the previous section, we have chosen the best pouch forming design, namely, a Aluswiss film with a pouch forming pressure of 27 psi. In this section, we examine other design aspects of the beef stew pouch. Particularly, we focus on the raw material target fill weights. In the military standard for the beef stew pouch, we have minimum weight requirements for the net weight and beef and vegetables drained weights. In addition, there are specifications for the fat content, the salt content and the connective tissue in the beef. Besides the finished product specifications, we might also have *in process* specifications or specifications that have to be adhered to due to the design of the process. As an example of such internal specifications, we

will discuss the maximum net weight requirement. The maximum net weight* (e.g. 250g) is one of the critical factors on which the thermal process design is based to ensure thorough sterilization of the food pouches. Though this requirement is not listed as one of finished product specifications, it is certainly an important in-process specification that the product/process should be designed to conform to. We summarize the specifications as follows (please refer to MIL-B-44059C):

Net Weight:	Individual pouch	≥ 212.6 g
	Average of 20	≥ 226.7 g
	Individual pouch	≤ 250 g (in-process specification)
Beef Drained Weight:	Individual pouch	≥ 56.7 g
	Average of 20	≥ 68.0 g
Vegetable Drained Weight:	Individual pouch	≥ 34.0 g
	Average of 20	≥ 45.3 g
Salt Content:	$0.5\% \leq$ Individual $\leq 1.3\%$	
Connective Tissue:	≤ 10.0 g	

Among the listed quality characteristics, the maximum net weight is the only one that is considered *critical* since any pouch exceeding the maximum weight could cause a failure of the thermal sterilization process and thus threatens the users' health. The remaining quality characteristics specifications, including the minimum net weight requirement for the net weight, are listed as *major* except the connective tissue, which is only considered *minor*. It is interesting to observe that the above specifications are somehow different from specifications we discussed in this report. For the weights and the fat content requirements, there are not only specifications for individual pouch but also specification for the average of a sample of 20 pouches. To calculate the PCI value, we take the minimum value of the PCI values for the individual and the average specifications. For example, the PCI value for the net weight minimum requirement is calculated as:

* For simplicity, we assume that the beef fill weight and the vegetable fill weight are not critical factors of the thermal process and are not bound by the in-process specifications.

$$PCI_{min_net} = \min\left[\frac{T_{net} - 212.6}{3\hat{\sigma}_{net}}, \frac{T_{net} - 226.7}{3\hat{\sigma}_{net} / \sqrt{20}}\right]$$

where T_{net} is the target fill weight of beef stew and $\hat{\sigma}_{net}$ is the estimated standard deviation of the individual pouch net weight. Similarly, we calculate the PCI values in the same fashion for other quality characteristics when both individual and average requirements are present.

It can also be observed that for the minimum weights requirements one can indefinitely increase the PCI values by increasing the target fill weights. However, the manufacturing cost will also be increased because of the extra amount of raw materials required. For the net weight specifications, increasing the PCI value for the minimum net weight requirement also diminishes the PCI value for the maximum net weight requirement. Our proposed producibility index will clearly demonstrate these tradeoffs. Before we calculate the producibility index, we first find out the relationships among the ingredients of the beef stew and the effects of the ingredient fill weights on the contents of *connective tissue, fat, and salt*. The beef stew is made of three ingredients: *gravy, beef, and vegetables*. There are three target fill weights that can be chosen by the manufacturer: *target pouch fill weight, target beef fill weight, and target vegetable fill weight*. Once these three fill weights are chosen, the following product characteristics are then calculated as:

Gravy fill weight = target pouch fill weight – target beef fill weight – target vegetable fill weight

Target beef drained weight = beef retort yield \times target beef fill weight
 $= 85\%^*$ target beef fill weight

Target vegetable drained weight = vegetable retort yield \times target vegetable fill weight
 $= 135\%^*$ target vegetable fill weight
 (dehydro frozen potato used)

Target salt content

$= 100\% \times (1.23\%^* \text{ target gravy fill weight} + 2.36\%^* \text{ target beef fill weight}) / \text{target pouch fill weight}$

* The numbers are based on estimates from experts.

Target weight of connective tissue = 6.5%* target beef drained weight

We conduct experiments to estimate the standard deviation for each quality characteristic. The results are shown in the following table:

Quality Characteristic	Estimated Standard Deviation
Net Weight (g)	4.57
Beef Drained Weight (g)	4.448
Vegetables Drained Weight (g)	8.33
Salt Content (%)	0.107
Connective Tissue (g)	0.507

It is found that the estimated standard deviations are not sensitive to the mean in the range of interest in our study. That is, changes in the target fill weights will not affect the estimated standard deviations for the listed quality characteristics. This is important since it would require additional experiments to estimate the standard deviations that are changed due to different fill weights. We now study the following two sets of the target fill weights:

Design #	Pouch Fill Weight	Beef fill Weight	Vegetable fill Wt.
A	232g	85g	51g
B	231g	87g	49g

We then calculate the PCI values in the following table:

Design #	Critical	Major					Minor	Unit Cost
		Max Net Weight	Min. Net Weight	Beef Drain Wt.	Veget. Drain Wt.	Salt Content		
A	1.313	1.415	1.155	1.395	1.194	3.485	1.192	
B	1.386	1.342	1.281	1.286	1.120	3.412	1.199	

* The numbers are based on estimates from experts.

Here, we take the maximum and minimum net weight requirements of design A as examples to demonstrate the calculations of PCI values:

$$PCI_{\max_net} = \frac{USL - T}{3\hat{\sigma}} = \frac{250 - 232}{3 \times 4.57} = 1.313 \text{ and}$$

$$PCI_{\min_net} = \min\left[\frac{232 - 212.6}{3 \times 4.57}, \frac{232 - 226.7}{3 \times 4.57 / \sqrt{20}}\right] = 1.415 .$$

Finally, we calculate the producibility index. Again, we take the design A as an example:

$$PCI_{critical} = \min[1.313] = 1.313;$$

$$PCI_{major} = \min[1.415, 1.155, 1.395, 1.194] = 1.155;$$

$$PCI_{minor} = \min[3.485] = 3.485 \text{ and}$$

$$PCI_{average} = [1.313^5 \times (1.415 \times 1.155 \times 1.395 \times 1.194)^{3/4} \times 3.485^1]^{1/(5+3+1)} = 1.453.$$

We use the importance ratio 5:3:1 for the calculation of average PCI. The following table shows the comparison of PI's between designs A and B:

Design	PI
	$[PCI_{critical}, PCI_{major}, PCI_{minor}, PCI_{average}, MC]$
A	$[1.313, 1.155, 3.485, 1.453, 1.192]$
B	$[1.386, 1.120, 3.412, 1.482, 1.199]$

It is interesting to observe that the second design (B) is an obvious attempt to correct the first design (A). In the first design, the PCI for the critical characteristic, maximum net weight, is not satisfactory. We thus decrease the pouch fill weight by 1 gram. Also, the PCI value for the beef drained weight is the minimum (1.155) among the major quality characteristics and is considered unacceptable. In the second design, we increase the beef fill weight and raise the PCI value for the beef drained weight to 1.28. In this design, the salt content becomes the major characteristic with the minimum PCI (1.12). This is, however, easily correctable by decreasing the salt content in the gravy. The manufacturing cost is also higher, by 0.7 cents, in the second

design due to the significant increase in the beef fill weight, the most expensive raw material. The PCI value for the connective tissue in this case is very high and does not concern us at all for the fill weights design. Now, it is up to the manufacturer to choose the better design. If both designs A and B are not acceptable, further developments of new designs may be necessary. Appendix F shows the spreadsheet program for the design B.

5.2 Producibility Index for the Ham Slice Pouches

In this section, we study different designs for the production of ham slice pouches. There are basically four different design settings:

- A: Hand Fill, Automatic Slicing,
- B: Hand Fill, Automatic Slicing/Sizing,
- C: Robot Fill, Automatic Slicing, and
- D: Robot Fill, Automatic Slicing/Sizing.

There are two filling designs: hand fill and robot fill. Two filling labors are required to place ham slices into the open pouches in order to meet the line speed: 60 pouches/minute. When robot is used to place the ham slices, it requires no labors. For both hand fill and robot fill, two labors are required to unpack the ham boxes and place the ham loafs on the slicer. These two labors are also responsible for sorting out broken slices or slices with unsatisfactory air pockets.

There are also two different designs in the ham slicing process. In the first design, the automatic slicing device cuts off ham slices from the ham loaf. In the second design, the slicer is also equipped with sizing device that cuts off the surface of the ham loaf to obtain more consistent shapes and weights of ham slices. The second design, however, increases the raw material cost by 10 cents per pound filled. The following table summarizes the differences in the elements of cost analysis resulting from the four designs:

Design	First Inspection Yield (%)	Ham Cost (\$/lb.)	Target Fill Weight (g)	No of Filling Labor	Capital Robot (\$)	Utility Cost Robot
A	96.3%	1.60	155	2	0.00	0.00
B	96.3%	1.70	145	2	0.00	0.00
C	94.4%	1.60	155	0	150,000	air: 5 ft ³ /hr elect: 5 kW
D	94.4%	1.70	145	0	150,000	air: 5 ft ³ /hr elect: 5 kW

Like beef stew pouches, the ham slice pouches have to go through two 100% inspections: one before and the other after the retort process. The robot appears to produce more defect pouches. This is possibly caused by the inaccuracy of the robot arm. The target fill weight for the slicing device is higher than the slicing/sizing device because the variations of resulted net weight and drained weight are higher without sizing. Again, we assume 99% efficiency of two 100% inspections on the pouch defects and calculate the defective level (%) of finished pouches using the following formula:

$$\text{Defective Level (\%)} = \left(\frac{1}{Yield_{first} \times Yield_{final}} - 1 \right) \left(\frac{1}{Inspection Efficiency} - 1 \right) \times 100\%$$

where $Yield_{first}$ is the yield from the first 100% inspection; $Yield_{final}$ is the yield from the final 100% inspection. An imaginary standard normal distribution with an upper specification limit is then established as discussed earlier:

$$\Psi(USL) = \frac{\text{Defective Level (\%)}}{100}.$$

Again, this quality characteristic is considered unilateral and the PCI can then be calculated as:

$$PCI = \frac{USL}{3}.$$

The results from the experiments are shown in the following table:

Design	Yield _{first}	Yield _{final}	Inspection Efficiency %	Defective Level %	PCI
A & B	0.963	0.99	99%	0.0494%	1.098
C & D	0.944	0.99	99%	0.0707%	1.064

As in the case of beef stew pouches, there are also specifications on the net weight and the drained weight (please refer to MIL-H-44063D):

Net Weight:	Individual pouch	≥ 113.4 g
	Average of 20	≥ 127.6 g
	Individual pouch	≤ 180 g (in-process specification)
Beef Drained Weight:	Individual pouch	≥ 102.1 g
	Average of 20	≥ 107.7 g

We again conduct experiments to gather data for estimating the standard deviations. The results are shown in the following table:

Design	Net Weight S.D.	Drained Wt. S.D.
A & C	7.795	7.692
B & D	3.199	5.851

Based on the above specifications and estimated standard deviations, we then calculate the PCI values. We summarize the results in the following table:

Design #	Critical		Major		Unit
	Max Net Wt.	Pouch Defect	Drain Wt.	Min Net Wt.	Cost
A	1.069	1.098	1.042	1.779	1.389
B	3.126	1.098	1.128	1.565	1.422
C	1.069	1.064	1.042	1.779	1.424
D	3.126	1.064	1.128	1.565	1.443

The producibility indices are then calculated:

Design #	PI
	$[PCI_{critical}, PCI_{major}, PCI_{minor}, PCI_{average}, MC]$
A	[1.069, 1.042, -, 1.180, 1.389]
B	[1.098, 1.128, -, 1.635, 1.422]
C	[1.069, 1.042, -, 1.169, 1.424]
D	[1.064, 1.128, -, 1.619, 1.443]

From the above comparisons, Design B, hand fill with slicing/sizing, appears to be the best design though the manufacturing cost is 3.3 cents higher than Design A. Appendix G shows the spreadsheet program for Design B.

6.0 Summary

We have developed a process producibility index which assesses the producibility of a product with given specifications. The index will determine whether the specifications of the product are producible (with acceptable cost) or not. We then demonstrated the application of this index to two MRE products, namely; beef stew pouches and sliced ham pouches.

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APPENDIX A
Estimate of ppm from N and r

N	r →									
	1	2	3	4	5	6	7	8	9	10
10	70233	168484	267886	367584	467402	567280	667193	767127	867076	967036
20	35117	84242	133943	183792	233701	283640	333596	383564	433538	483518
30	23411	56161	89295	122528	155801	189093	222398	255709	289025	322345
40	17558	42121	66971	91896	116850	141820	166798	191782	216769	241759
50	14047	33697	53577	73517	93480	113456	133439	153425	173415	193407
60	11706	28081	44648	61264	77900	94547	111199	127855	144513	161173
70	10033	24069	38269	52512	66772	81040	95313	109590	123868	138148
80	8779	21061	33486	45948	58425	70910	83399	95891	108385	120879
90	7804	18720	29765	40843	51934	63031	74133	85236	96342	107448
100	7023	16848	26789	36758	46740	56728	66719	76713	86708	96704
150	4682	11232	17859	24506	31160	37819	44480	51142	57805	64469
200	3512	8424	13394	18379	23370	28364	33360	38356	43354	48352
250	2809	6739	10715	14703	18696	22691	26688	30685	34683	38681
300	2341	5616	8930	12253	15580	18909	22240	25571	28903	32235
350	2007	4814	7654	10502	13354	16208	19063	21918	24774	27630
400	1756	4212	6697	9190	11685	14182	16680	19178	21677	24176
450	1561	3744	5953	8169	10387	12606	14827	17047	19268	21490
500	1405	3370	5358	7352	9348	11346	13344	15343	17342	19341
600	1171	2808	4465	6126	7790	9455	11120	12785	14451	16117
700	1003	2407	3827	5251	6677	8104	9531	10959	12387	13815
800	878	2106	3349	4595	5843	7091	8340	9589	10838	12088
900	780	1872	2977	4084	5193	6303	7413	8524	9634	10745
1,000	702	1685	2679	3676	4674	5673	6672	7671	8671	9670
1,100	638	1532	2435	3342	4249	5157	6065	6974	7883	8791
1,200	585	1404	2232	3063	3895	4727	5560	6393	7226	8059
1,300	540	1296	2061	2828	3595	4364	5132	5901	6670	7439
1,400	502	1203	1913	2626	3339	4052	4766	5479	6193	6907
1,500	468	1123	1786	2451	3116	3782	4448	5114	5781	6447
1,600	439	1053	1674	2297	2921	3546	4170	4795	5419	6044
1,700	413	991	1576	2162	2749	3337	3925	4513	5100	5688
1,800	390	936	1488	2042	2597	3152	3707	4262	4817	5372
1,900	370	887	1410	1935	2460	2986	3512	4038	4564	5090
2,000	351	842	1339	1838	2337	2836	3336	3836	4335	4835
2,200	319	766	1218	1671	2125	2579	3033	3487	3941	4396
2,400	293	702	1116	1532	1948	2364	2780	3196	3613	4029
2,600	270	648	1030	1414	1798	2182	2566	2950	3335	3719
2,800	251	602	957	1313	1669	2026	2383	2740	3097	3454
3,000	234	562	893	1225	1558	1891	2224	2557	2890	3223
3,200	219	527	837	1149	1461	1773	2085	2397	2710	3022
3,400	207	496	788	1081	1375	1668	1962	2256	2550	2844
3,600	195	468	744	1021	1298	1576	1853	2131	2409	2686
3,800	185	443	705	967	1230	1493	1756	2019	2282	2545
4,000	176	421	670	919	1169	1418	1668	1918	2168	2418
4,200	167	401	638	875	1113	1351	1589	1826	2064	2302
4,400	160	383	609	835	1062	1289	1516	1743	1971	2198
4,600	153	366	582	799	1016	1233	1450	1668	1885	2102
4,800	146	351	558	766	974	1182	1390	1598	1806	2015
5,000	140	337	536	735	935	1135	1334	1534	1734	1934
5,500	128	306	487	668	850	1031	1213	1395	1577	1758
6,000	117	281	446	613	779	945	1112	1279	1445	1612

N = a unit of product, an opportunity for nonconformities, etc.

r = the number of nonconformities.

N	1	2	3	4	5	6	7	8	9	10
6,500	108	259	412	566	719	873	1026	1180	1334	1488
7,000	100	241	383	525	668	810	953	1096	1239	1381
7,500	94	225	357	490	623	756	890	1023	1156	1289
8,000	88	211	335	459	584	709	834	959	1084	1209
8,500	83	198	315	432	550	667	785	903	1020	1138
9,000	78	187	298	408	519	630	741	852	963	1074
9,500	74	177	282	387	492	597	702	808	913	1018
10,000	70	168	268	368	467	567	667	767	867	967
11,000	64	153	244	334	425	516	607	697	788	879
12,000	59	140	223	306	390	473	556	639	723	806
13,000	54	130	206	283	360	436	513	590	667	744
14,000	50	120	191	263	334	405	477	548	619	691
15,000	47	112	179	245	312	378	445	511	578	645
16,000	44	105	167	230	292	355	417	479	542	604
17,000	41	99	158	216	275	334	392	451	510	569
18,000	39	94	149	204	260	315	371	426	482	537
19,000	37	89	141	193	246	299	351	404	456	509
20,000	35	84	134	184	234	284	334	384	434	484
25,000	28	67	107	147	187	227	267	307	347	387
30,000	23	56	89	123	156	189	222	256	289	322
35,000	20	48	77	105	134	162	191	219	248	276
40,000	18	42	67	92	117	142	167	192	217	242
45,000	16	37	60	82	104	126	148	170	193	215
50,000	14	34	54	74	93	113	133	153	173	193
55,000	13	31	49	67	85	103	121	139	158	176
60,000	12	28	45	61	78	95	111	128	145	161
65,000	11	26	41	57	72	87	103	118	133	149
70,000	10	24	38	53	67	81	95	110	124	138
75,000	9.4	22	36	49	62	76	89	102	116	129
80,000	8.8	21	33	46	58	71	83	96	108	121
85,000	8.3	20	32	43	55	67	78	90	102	114
90,000	7.8	19	30	41	52	63	74	85	96	107
95,000	7.4	18	28	39	49	60	70	81	91	102
100,000	7.0	17	27	37	47	57	67	77	87	97
105,000	6.7	16	26	35	45	54	64	73	83	92
110,000	6.4	15	24	33	42	52	61	70	79	88
120,000	5.9	14	22	31	39	47	56	64	72	81
130,000	5.4	13	21	28	36	44	51	59	67	74
140,000	5.0	12	19	26	33	41	48	55	62	69
150,000	4.7	11	18	25	31	38	44	51	58	64
160,000	4.4	10.5	17	23	29	35	42	48	54	60
170,000	4.1	9.9	16	22	27	33	39	45	51	57
180,000	3.9	9.4	15	20	26	32	37	43	48	54
190,000	3.7	8.9	14	19	25	30	35	40	46	51
200,000	3.5	8.4	13	18	23	28	33	38	43	48
210,000	3.3	8.0	12.8	18	22	27	32	37	41	46
220,000	3.2	7.7	12.2	17	21	26	30	35	39	44
230,000	3.1	7.3	11.6	16	20	25	29	33	38	42
240,000	2.9	7.0	11.2	15	19	24	28	32	36	40
250,000	2.8	6.7	10.7	14.7	18.7	23	27	31	35	39

N = a unit of product, an opportunity for nonconformities, etc.

r = the number of nonconformities.

N	r →									
	1	2	3	4	5	6	7	8	9	10
260,000	2.7	6.5	10.3	14.1	18.0	22	26	30	33	37
270,000	2.6	6.2	9.9	13.6	17.3	21	25	28	32	36
280,000	2.5	6.0	9.6	13.1	16.7	20	24	27	31	35
290,000	2.4	5.8	9.2	12.7	16.1	19.6	23	26	30	33
300,000	2.3	5.6	8.9	12.3	15.6	18.9	22	26	29	32
310,000	2.27	5.4	8.6	11.9	15.1	18.3	22	25	28	31
320,000	2.19	5.3	8.4	11.5	14.6	17.7	21	24	27	30
330,000	2.13	5.1	8.1	11.1	14.2	17.2	20	23	26	29
340,000	2.07	5.0	7.9	10.8	13.7	16.7	19.6	23	26	28
350,000	2.01	4.8	7.7	10.5	13.4	16.2	19.1	22	25	28
360,000	1.95	4.7	7.4	10.2	13.0	15.8	18.5	21	24	27
370,000	1.90	4.6	7.2	9.9	12.6	15.3	18.0	21	23	26
380,000	1.85	4.4	7.0	9.7	12.3	14.9	17.6	20.2	23	25
390,000	1.80	4.3	6.9	9.4	12.0	14.5	17.1	19.7	22	25
400,000	1.76	4.2	6.7	9.2	11.7	14.2	16.7	19.2	22	24
450,000	1.56	3.7	6.0	8.2	10.4	12.6	14.8	17.0	19	21
500,000	1.40	3.4	5.4	7.4	9.3	11.3	13.3	15.3	17	19
550,000	1.28	3.1	4.9	6.7	8.5	10.3	12.1	13.9	16	18
600,000	1.17	2.8	4.5	6.1	7.8	9.5	11.1	12.8	14	16
650,000	1.08	2.6	4.1	5.7	7.2	8.7	10.3	11.8	13	15
700,000	1.00	2.4	3.8	5.3	6.7	8.1	9.5	11.0	12.4	14
750,000	0.94	2.2	3.6	4.9	6.2	7.6	8.9	10.2	11.6	13
800,000	0.88	2.1	3.3	4.6	5.8	7.1	8.3	9.6	10.8	12
850,000	0.83	2.0	3.2	4.3	5.5	6.7	7.8	9.0	10.2	11
900,000	0.78	1.9	3.0	4.1	5.2	6.3	7.4	8.5	9.6	10.7
950,000	0.74	1.8	2.8	3.9	4.9	6.0	7.0	8.1	9.1	10.2
1,000,000	0.70	1.7	2.7	3.7	4.7	5.7	6.7	7.7	8.7	9.7

N = a unit of product, an opportunity for nonconformities, etc.

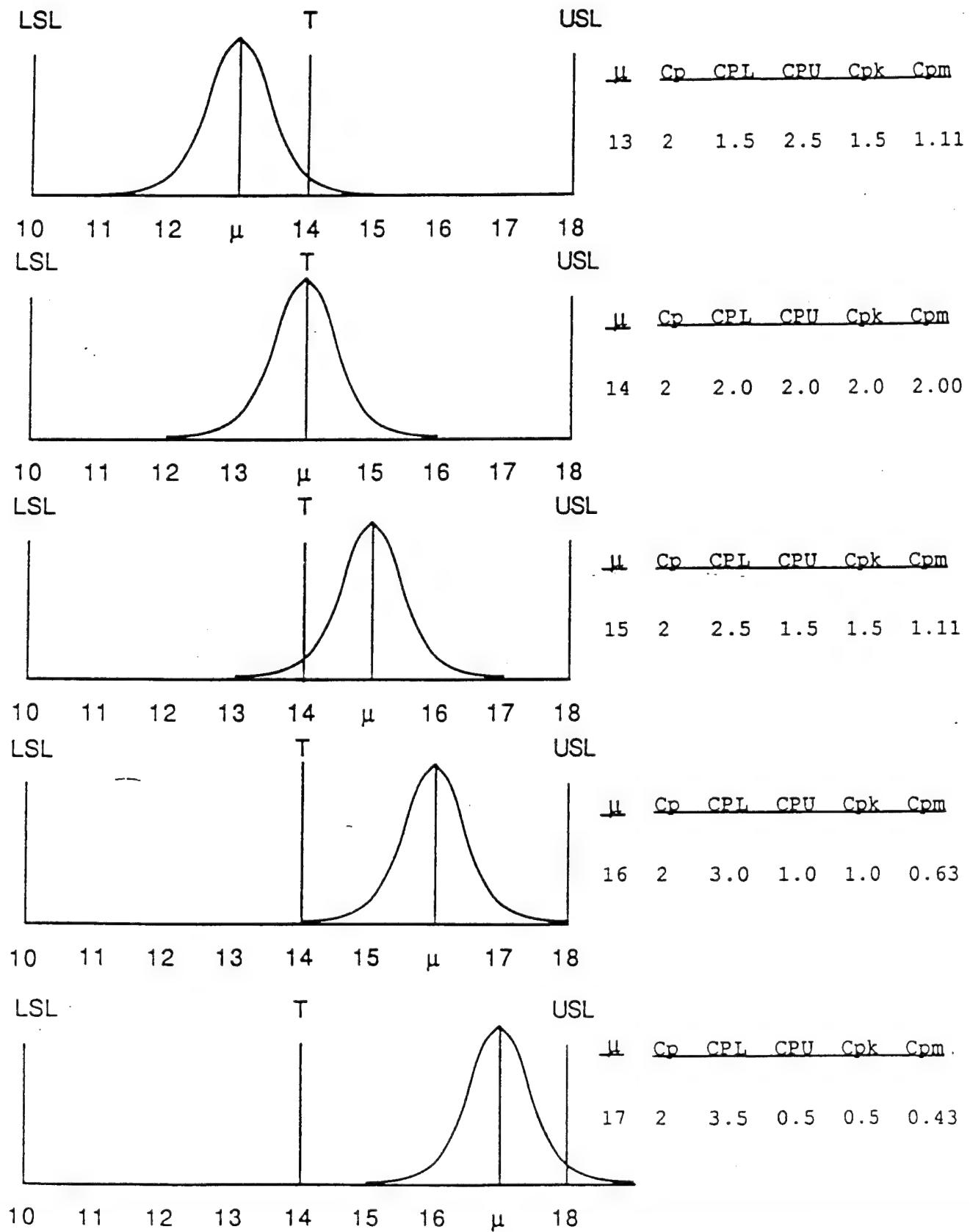
r = the number of nonconformities.

APPENDIX B
Area under Standard Normal Distribution Curve
Beyon a selected value z

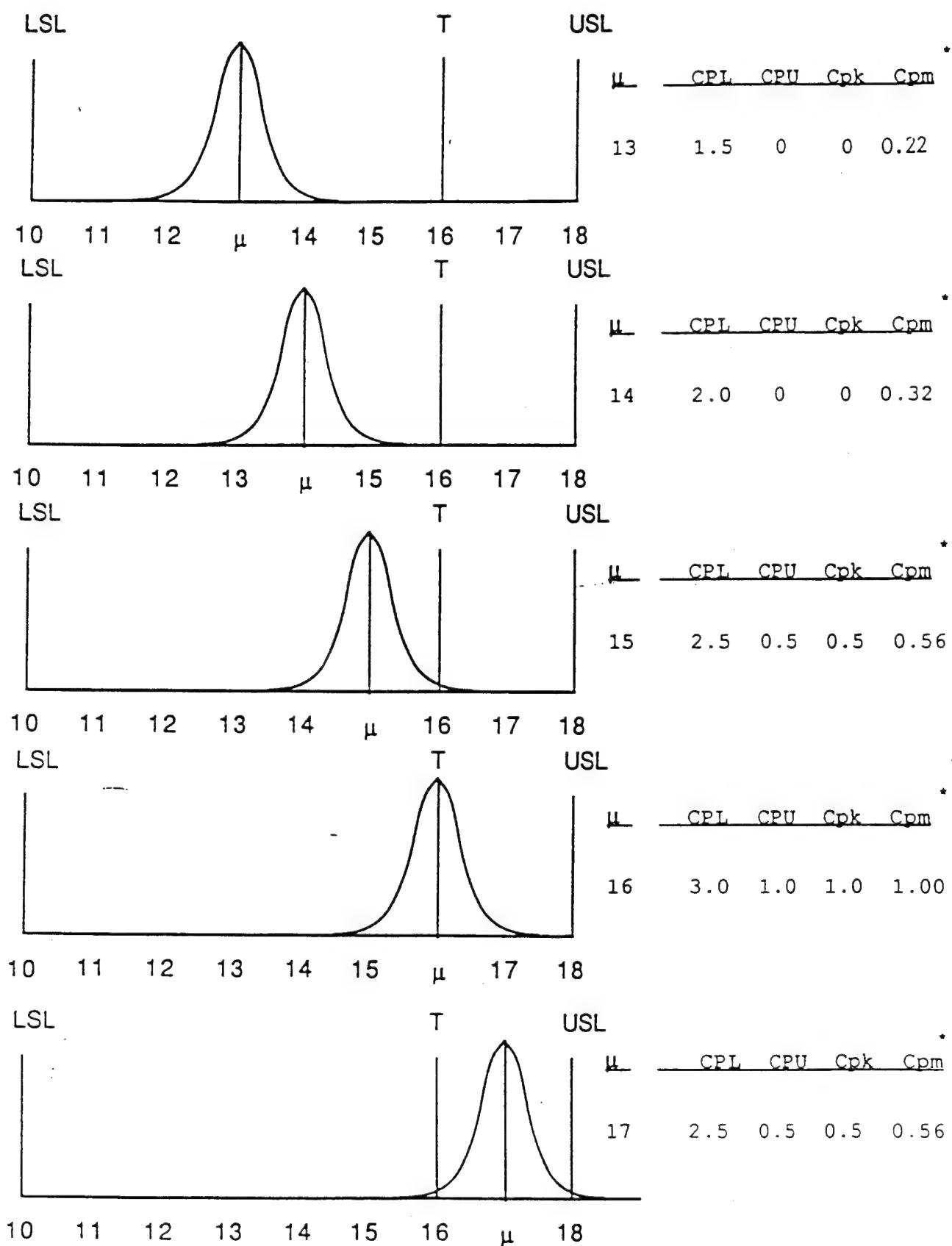
z	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.00	5.000E-01	4.960E-01	4.920E-01	4.880E-01	4.840E-01	4.801E-01	4.761E-01	4.721E-01	4.681E-01	4.641E-01
0.10	4.602E-01	4.562E-01	4.522E-01	4.483E-01	4.443E-01	4.404E-01	4.364E-01	4.325E-01	4.286E-01	4.247E-01
0.20	4.207E-01	4.168E-01	4.129E-01	4.090E-01	4.052E-01	4.013E-01	3.974E-01	3.936E-01	3.897E-01	3.859E-01
0.30	3.821E-01	3.783E-01	3.745E-01	3.707E-01	3.669E-01	3.632E-01	3.594E-01	3.557E-01	3.520E-01	3.483E-01
0.40	3.446E-01	3.409E-01	3.372E-01	3.336E-01	3.300E-01	3.264E-01	3.228E-01	3.192E-01	3.156E-01	3.121E-01
0.50	3.085E-01	3.050E-01	3.015E-01	2.981E-01	2.946E-01	2.912E-01	2.877E-01	2.843E-01	2.810E-01	2.776E-01
0.60	2.743E-01	2.709E-01	2.676E-01	2.643E-01	2.611E-01	2.578E-01	2.546E-01	2.514E-01	2.483E-01	2.451E-01
0.70	2.420E-01	2.389E-01	2.358E-01	2.327E-01	2.297E-01	2.266E-01	2.236E-01	2.207E-01	2.177E-01	2.148E-01
0.80	2.119E-01	2.090E-01	2.061E-01	2.033E-01	2.005E-01	1.977E-01	1.949E-01	1.922E-01	1.894E-01	1.867E-01
0.90	1.841E-01	1.814E-01	1.788E-01	1.762E-01	1.736E-01	1.711E-01	1.685E-01	1.660E-01	1.635E-01	1.611E-01
1.00	1.587E-01	1.562E-01	1.539E-01	1.515E-01	1.492E-01	1.469E-01	1.446E-01	1.423E-01	1.401E-01	1.379E-01
1.10	1.357E-01	1.335E-01	1.314E-01	1.292E-01	1.271E-01	1.251E-01	1.230E-01	1.210E-01	1.190E-01	1.170E-01
1.20	1.151E-01	1.131E-01	1.112E-01	1.093E-01	1.075E-01	1.056E-01	1.038E-01	1.020E-01	1.003E-01	9.853E-02
1.30	9.680E-02	9.510E-02	9.342E-02	9.176E-02	9.012E-02	8.851E-02	8.691E-02	8.534E-02	8.379E-02	8.226E-02
1.40	8.076E-02	7.927E-02	7.780E-02	7.636E-02	7.493E-02	7.353E-02	7.214E-02	7.078E-02	6.944E-02	6.811E-02
1.50	6.681E-02	6.552E-02	6.426E-02	6.301E-02	6.178E-02	6.057E-02	5.938E-02	5.821E-02	5.705E-02	5.592E-02
1.60	5.480E-02	5.370E-02	5.262E-02	5.155E-02	5.050E-02	4.947E-02	4.846E-02	4.746E-02	4.648E-02	4.551E-02
1.70	4.457E-02	4.363E-02	4.272E-02	4.182E-02	4.093E-02	4.006E-02	3.920E-02	3.836E-02	3.754E-02	3.673E-02
1.80	3.593E-02	3.515E-02	3.438E-02	3.363E-02	3.288E-02	3.216E-02	3.144E-02	3.074E-02	3.005E-02	2.938E-02
1.90	2.872E-02	2.807E-02	2.743E-02	2.680E-02	2.619E-02	2.559E-02	2.500E-02	2.442E-02	2.385E-02	2.330E-02
2.00	2.275E-02	2.222E-02	2.169E-02	2.118E-02	2.068E-02	2.018E-02	1.970E-02	1.923E-02	1.876E-02	1.831E-02
2.10	1.786E-02	1.743E-02	1.700E-02	1.659E-02	1.618E-02	1.578E-02	1.539E-02	1.500E-02	1.463E-02	1.426E-02
2.20	1.390E-02	1.355E-02	1.321E-02	1.287E-02	1.255E-02	1.222E-02	1.191E-02	1.160E-02	1.130E-02	1.101E-02
2.30	1.072E-02	1.044E-02	1.017E-02	9.903E-03	9.643E-03	9.387E-03	9.137E-03	8.894E-03	8.656E-03	8.424E-03
2.40	8.198E-03	7.976E-03	7.760E-03	7.549E-03	7.344E-03	7.143E-03	6.947E-03	6.756E-03	6.569E-03	6.387E-03
2.50	6.210E-03	6.036E-03	5.868E-03	5.703E-03	5.543E-03	5.386E-03	5.234E-03	5.085E-03	4.940E-03	4.799E-03
2.60	4.661E-03	4.527E-03	4.396E-03	4.269E-03	4.145E-03	4.024E-03	3.907E-03	3.792E-03	3.681E-03	3.572E-03
2.70	3.467E-03	3.364E-03	3.264E-03	3.167E-03	3.072E-03	2.980E-03	2.890E-03	2.803E-03	2.718E-03	2.675E-03
2.80	2.555E-03	2.477E-03	2.401E-03	2.327E-03	2.256E-03	2.186E-03	2.118E-03	2.052E-03	1.988E-03	1.926E-03
2.90	1.866E-03	1.807E-03	1.750E-03	1.695E-03	1.641E-03	1.589E-03	1.538E-03	1.489E-03	1.441E-03	1.395E-03
3.00	1.350E-03	1.306E-03	1.264E-03	1.223E-03	1.183E-03	1.144E-03	1.107E-03	1.070E-03	1.035E-03	1.001E-03
3.10	9.676E-04	9.354E-04	9.042E-04	8.740E-04	8.447E-04	8.163E-04	7.888E-04	7.622E-04	7.364E-04	7.114E-04
3.20	6.871E-04	6.637E-04	6.410E-04	6.190E-04	5.977E-04	5.770E-04	5.571E-04	5.378E-04	5.191E-04	5.010E-04
3.30	4.835E-04	4.665E-04	4.501E-04	4.343E-04	4.189E-04	4.041E-04	3.898E-04	3.759E-04	3.625E-04	3.495E-04
3.40	3.370E-04	3.249E-04	3.132E-04	3.019E-04	2.909E-04	2.804E-04	2.702E-04	2.603E-04	2.508E-04	2.416E-04
3.50	2.327E-04	2.242E-04	2.159E-04	2.079E-04	2.002E-04	1.927E-04	1.855E-04	1.786E-04	1.719E-04	1.655E-04
3.60	1.592E-04	1.532E-04	1.474E-04	1.415E-04	1.364E-04	1.312E-04	1.262E-04	1.214E-04	1.167E-04	1.123E-04
3.70	1.079E-04	1.038E-04	9.974E-05	9.587E-05	9.214E-05	8.855E-05	8.509E-05	8.175E-05	7.854E-05	7.545E-05
3.80	7.248E-05	6.961E-05	6.685E-05	6.420E-05	6.165E-05	5.919E-05	5.682E-05	5.455E-05	5.236E-05	5.029E-05
3.90	4.822E-05	4.627E-05	4.440E-05	4.260E-05	4.086E-05	3.920E-05	3.760E-05	3.606E-05	3.458E-05	3.316E-05
4.00	3.179E-05	3.048E-05	2.921E-05	2.800E-05	2.684E-05	2.572E-05	2.465E-05	2.362E-05	2.263E-05	2.168E-05
4.10	2.076E-05	1.989E-05	1.905E-05	1.824E-05	1.747E-05	1.672E-05	1.601E-05	1.533E-05	1.467E-05	1.404E-05
4.20	1.344E-05	1.286E-05	1.231E-05	1.177E-05	1.126E-05	1.077E-05	1.031E-05	9.857E-06	9.426E-06	9.014E-06
4.30	8.619E-06	8.240E-06	7.878E-06	7.530E-06	7.198E-06	6.879E-06	6.574E-06	6.282E-06	6.002E-06	5.734E-06
4.40	5.478E-06	5.233E-06	4.998E-06	4.773E-06	4.558E-06	4.353E-06	4.156E-06	3.968E-06	3.787E-06	3.615E-06
4.50	3.451E-06	3.293E-06	3.143E-06	2.999E-06	2.861E-06	2.730E-06	2.604E-06	2.484E-06	2.369E-06	2.259E-06
4.60	2.154E-06	2.054E-06	1.959E-06	1.867E-06	1.780E-06	1.697E-06	1.617E-06	1.541E-06	1.469E-06	1.399E-06
4.70	1.333E-06	1.270E-06	1.210E-06	1.153E-06	1.098E-06	1.046E-06	9.956E-07	9.480E-07	9.026E-07	8.593E-07
4.80	8.181E-07	7.787E-07	7.411E-07	7.054E-07	6.712E-07	6.387E-07	6.077E-07	5.782E-07	5.500E-07	5.233E-07
4.90	4.976E-07	4.733E-07	4.501E-07	4.280E-07	4.070E-07	3.869E-07	3.678E-07	3.496E-07	3.323E-07	3.159E-07

Z	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
5.00	3.002E-07	3.853E-07	2.711E-07	2.575E-07	2.447E-07	2.324E-07	2.208E-07	2.097E-07	1.991E-07	1.891E-07
5.10	1.796E-07	1.705E-07	1.619E-07	1.537E-07	1.459E-07	1.385E-07	1.314E-07	1.247E-07	1.184E-07	1.123E-07
5.20	1.066E-07	1.011E-07	9.591E-08	9.098E-08	8.629E-08	8.184E-08	7.762E-08	7.360E-08	6.979E-08	6.617E-08
5.30	6.273E-08	5.947E-08	5.637E-08	5.343E-08	5.064E-08	4.799E-08	4.548E-08	4.309E-08	4.083E-08	3.868E-08
5.40	3.664E-08	3.471E-08	3.288E-08	3.114E-08	2.949E-08	2.792E-08	2.644E-08	2.503E-08	2.370E-08	2.244E-08
5.50	2.124E-08	2.010E-08	1.903E-08	1.801E-08	1.704E-08	1.613E-08	1.526E-08	1.444E-08	1.366E-08	1.292E-08
5.60	1.222E-08	1.156E-08	1.093E-08	1.034E-08	9.776E-09	9.244E-09	8.741E-09	8.264E-09	7.812E-09	7.385E-09
5.70	6.980E-09	6.598E-09	6.235E-09	5.893E-09	5.568E-09	5.262E-09	4.971E-09	4.697E-09	4.437E-09	4.191E-09
5.80	3.959E-09	3.739E-09	3.532E-09	3.335E-09	3.150E-09	2.974E-09	2.808E-09	2.651E-09	2.503E-09	2.363E-09
5.90	2.230E-09	2.105E-09	1.987E-09	1.875E-09	1.769E-09	1.670E-09	1.576E-09	1.487E-09	1.402E-09	1.323E-09
6.00	1.248E-09	1.177E-09	1.110E-09	1.047E-09	9.876E-10	9.314E-10	8.783E-10	8.281E-10	7.808E-10	7.361E-10
6.10	6.940E-10	6.542E-10	6.166E-10	5.812E-10	5.478E-10	5.163E-10	4.865E-10	4.585E-10	4.320E-10	4.070E-10
6.20	3.835E-10	3.613E-10	3.403E-10	3.206E-10	3.020E-10	2.844E-10	2.679E-10	2.523E-10	2.376E-10	2.237E-10
6.30	2.107E-10	1.983E-10	1.867E-10	1.758E-10	1.655E-10	1.558E-10	1.466E-10	1.380E-10	1.299E-10	1.223E-10
6.40	1.151E-10	1.083E-10	1.019E-10	9.586E-11	9.020E-11	8.486E-11	7.983E-11	7.510E-11	7.064E-11	6.645E-11
6.50	6.250E-11	5.878E-11	5.529E-11	5.199E-11	4.889E-11	4.597E-11	4.323E-11	4.065E-11	3.821E-11	3.593E-11
6.60	3.377E-11	3.175E-11	2.984E-11	2.805E-11	2.637E-11	2.478E-11	2.329E-11	2.189E-11	2.057E-11	1.933E-11
6.70	1.816E-11	1.706E-11	1.603E-11	1.506E-11	1.415E-11	1.329E-11	1.249E-11	1.173E-11	1.102E-11	1.035E-11
6.80	9.719E-12	9.127E-12	8.572E-12	8.049E-12	7.559E-12	7.097E-12	6.664E-12	6.257E-12	5.874E-12	5.515E-12
6.90	5.178E-12	4.860E-12	4.562E-12	4.283E-12	4.020E-12	3.773E-12	3.541E-12	3.323E-12	3.119E-12	2.927E-12
7.00	2.747E-12	2.577E-12	2.418E-12	2.269E-12	2.129E-12	1.997E-12	1.874E-12	1.758E-12	1.649E-12	1.547E-12
7.10	1.451E-12	1.361E-12	1.277E-12	1.198E-12	1.123E-12	1.053E-12	9.879E-13	9.264E-13	8.688E-13	8.147E-13
7.20	7.639E-13	7.163E-13	6.716E-13	6.297E-13	5.904E-13	5.535E-13	5.189E-13	4.864E-13	4.560E-13	4.275E-13
7.30	4.007E-13	3.756E-13	3.520E-13	3.300E-13	3.092E-13	2.898E-13	2.716E-13	2.546E-13	2.386E-13	2.235E-13
7.40	2.095E-13	1.963E-13	1.839E-13	1.733E-13	1.615E-13	1.513E-13	1.417E-13	1.328E-13	1.244E-13	1.166E-13
7.50	1.092E-13	1.023E-13	9.581E-14	8.975E-14	8.407E-14	7.874E-14	7.375E-14	6.908E-14	6.470E-14	6.060E-14
7.60	5.675E-14	5.315E-14	4.977E-14	4.661E-14	4.365E-14	4.087E-14	3.827E-14	3.584E-14	3.356E-14	3.142E-14
7.70	2.942E-14	2.755E-14	2.579E-14	2.415E-14	2.261E-14	2.116E-14	1.981E-14	1.855E-14	1.736E-14	1.625E-14
7.80	1.522E-14	1.424E-14	1.333E-14	1.248E-14	1.168E-14	1.093E-14	1.023E-14	9.579E-15	8.965E-15	8.391E-15
7.90	7.853E-15	7.349E-15	6.878E-15	6.437E-15	6.024E-15	5.637E-15	5.275E-15	4.937E-15	4.620E-15	4.323E-15
8.00	4.045E-15	3.785E-15	3.542E-15	3.314E-15	3.101E-15	2.901E-15	2.715E-15	2.540E-15	2.376E-15	2.223E-15
8.10	2.080E-15	1.946E-15	1.821E-15	1.703E-15	1.593E-15	1.491E-15	1.395E-15	1.305E-15	1.220E-15	1.142E-15
8.20	1.068E-15	9.991E-16	9.346E-16	8.742E-16	8.177E-16	7.649E-16	7.155E-16	6.692E-16	6.260E-16	5.855E-16
8.30	5.477E-16	5.122E-16	4.791E-16	4.481E-16	4.191E-16	3.920E-16	3.666E-16	3.429E-16	3.207E-16	2.999E-16
8.40	2.805E-16	2.524E-16	2.454E-16	2.295E-16	2.146E-16	2.007E-16	1.877E-16	1.755E-16	1.642E-16	1.535E-16
8.50	1.436E-16	1.342E-16	1.255E-16	1.174E-16	1.098E-16	1.027E-16	9.601E-17	8.978E-17	8.395E-17	7.851E-17
8.60	7.341E-17	6.865E-17	6.419E-17	6.003E-17	5.613E-17	5.249E-17	4.908E-17	4.589E-17	4.291E-17	4.013E-17
8.70	3.752E-17	3.508E-17	3.281E-17	3.068E-17	2.868E-17	2.682E-17	2.508E-17	2.345E-17	2.193E-17	2.050E-17
8.80	1.917E-17	1.792E-17	1.676E-17	1.567E-17	1.465E-17	1.370E-17	1.281E-17	1.198E-17	1.120E-17	1.047E-17
8.90	9.792E-18	9.155E-18	8.560E-18	8.004E-18	7.484E-18	6.998E-18	6.543E-18	6.118E-18	5.720E-18	5.349E-18
9.00	5.001E-18	4.676E-18	4.372E-18	4.088E-18	3.823E-18	3.574E-18	3.342E-18	3.125E-18	2.922E-18	2.732E-18
9.10	2.555E-18	2.389E-18	2.234E-18	2.089E-18	1.953E-18	1.826E-18	1.707E-18	1.597E-18	1.493E-18	1.396E-18
9.20	1.305E-18	1.221E-18	1.141E-18	1.067E-18	9.979E-19	9.332E-19	8.726E-19	8.160E-19	7.630E-19	7.135E-19
9.30	6.672E-19	6.239E-19	5.834E-19	5.456E-19	5.102E-19	4.771E-19	4.462E-19	4.172E-19	3.902E-19	3.649E-19
9.40	3.412E-19	3.191E-19	2.984E-19	2.791E-19	2.610E-19	2.441E-19	2.283E-19	2.135E-19	1.996E-19	1.867E-19
9.50	1.746E-19	1.633E-19	1.527E-19	1.428E-19	1.336E-19	1.250E-19	1.169E-19	1.093E-19	1.022E-19	9.562E-20
9.60	8.943E-20	8.365E-20	7.824E-20	7.318E-20	6.845E-20	6.402E-20	5.988E-20	5.601E-20	5.240E-20	4.901E-20
9.70	4.584E-20	4.288E-20	4.011E-20	3.752E-20	3.510E-20	3.284E-20	3.072E-20	2.873E-20	2.688E-20	2.515E-20
9.80	2.352E-20	2.021E-20	2.059E-20	1.926E-20	1.802E-20	1.686E-20	1.577E-20	1.476E-20	1.381E-20	1.292E-20
9.90	1.209E-20	1.131E-20	1.058E-20	9.898E-21	9.262E-21	8.666E-21	8.108E-21	7.587E-21	7.099E-21	6.643E-21
10.00	6.216E-21	5.817E-21	5.443E-21	5.093E-21	4.766E-21	4.460E-21	4.174E-21	3.906E-21	3.655E-21	3.421E-21

APPENDIX C
Comparson among Four PCI measures



Comparisons of C_p , C_{pk} , C_{PL} , C_{PU} , and C_{pm} with $(USL - T) = (T - LSL)$.



Comparisons of C_{pk} , CPU, CPL, and C_{pm}^* with $(USL - T) \neq (T - LSL)$.

APPENDIX D
SpreadSheet: Cost Analysis for Pouch Forming Design C

Production Schedule

Hours/Shift	8
Shifts/Day	1
Days/Week	5
Weeks/Year	48
Hours/Year	1920
Production Rate MRE Line	
Units/Minute	102
Avg Unit Fill&Seal/Hour	4,651
Avg Unit for Fill / Hour with rework	4,455
Avg Unit FP Output Rate/Hour	4,250
Daily Unit Rate	34,001
Annual Output from Final Inspect	8,242,671
Annualized Unit Rate	8,160,244
Annual Requirement	5,000,000
Plant Utilization	61.27%

Process Yield & Efficiency

	Efficiency	Yield
Product Preparation Equipm.	90.0%	95.0% (yield of gravy system)
Filling Equipment	95.0%	97.0% (avg yield of product)
Horizontal Form & Seal Equipment	80.0%	90.0% (yield of packaging materia
Pouch Packaging System	76.0%	
First Inspection Equipment	90.0%	92.3% (% accepted pouches)
Rework System	80.0%	95.0%
Rack Loading Equipment	90.0%	100.0%
Retort Equipment	90.0%	100.0%
Rack Unloading Equipment	90.0%	100.0%
Final Inspection Equipment	90.0%	100.0% (% accepted pouches)
Final Packaging Equipment	70.0%	99.0% (% yield including qc samp

	Rated Capacity	Output Expected
Process Design Capacity		
Product Preparation Equipment	86.6	74.1 pouches/min
Filling Equipment	102.0	77.5 pouches/min
Horizontal Form & Seal Equipment	102.0	77.5 pouches/min
First Inspection Equipment	113.3	71.6 inspections/min
Rework System	9.8	5.7
Rack Loading Equipment	113.3	71.6 pouches/min
Retort Equipment	113.3	71.6 pouches/min
Rack Unloading Equipment	113.3	71.6 pouches/min
Final Inspection Equipment	113.3	71.6 inspections/min
Final Packaging Equipment	145.7	70.8 pouches/min

Material Data Cost Sheet

Product Ingredient	Formula	% Formula	Preparation Yield%	Cost/lb	Cost/Lb	Fat Cont%	Salt Cont%	Drain Wt. Yield%
Gravy	96.46	41.80%	95.00%	\$0.15	\$0.066	3.60%	0.12%	
Beef Fill Wt	83.33	36.11%	95.00%	\$2.00	\$0.760	0.65%	2.36%	85.00%
Veg. Fill Wt	50.98	22.09%						135.00%
Potato	21.300836	9.23%	95.00%	\$0.70	\$0.068			
Carrots	21.300836	9.23%	95.00%	\$0.65	\$0.063			
Peas	8.3783287	3.63%	95.00%	\$0.85	\$0.032			
	=====	=====		=====	=====			
	230.77	100.00%			\$0.990			

Avg Target Fill Weight [gram]
[lb] 230.77
0.5096511

Product Cost/Container **\$0.504**

Packaging Material

	\$/m	pouches/m	% yield	\$/pouch
Top Film	\$0.71	16.528926	90.0%	\$0.048
Bottom Film	\$0.71	16.528926	90.0%	\$0.048
	=====	=====		=====
		Pouch Cost		\$0.096

	\$/unit	pouch/unit	% yield	\$/pouch
Carton	\$0.07	1	99.00%	\$0.074
Case	\$0.34	72	99.00%	\$0.005
Inserts	\$0.23	72	99.00%	\$0.003
Pallet	\$10.00	2880	99.00%	\$0.003
	=====	=====		=====
		FP Packaging Cost		\$0.085

Labor Cost Estimate

	Rate	Wages
Warehouse Labor	2	\$20.00
Gravy Prep Labor	1	\$10.00
Filling Labor	1	\$10.00
Packaging Labor	1	\$15.00
First Inspection	6	\$60.00
Rework Labor	1	\$10.00
Rack Loading	4	\$40.00
Retort Labor	2	\$30.00
Rack Unloading & Washing	3	\$30.00
Final Inspection Labor	12	\$120.00
Finished Product Packaging	2	\$20.00
Cleaning Labor	3	\$30.00

===== ===== =====

Total Labor / Hr	38	\$395.00
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Annual Opperating Labor Cost	\$758,400.00
Direct Supervisory and Clerical I	15.00% OL
Quality Control	15.00% OL

===== ===== =====

Total Annual Labor Cost	\$985,920
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Assumptions Labor:	sec/inspec	inspector
First Inspection Time	3	5.7
Second Inspection Time	6	11.3

	p/man/min	
Rack Loading	30	3.8
Rack Unloading	40	2.8

	p/man/min	
Rework Labor	10	1.0

Capital Equipment

Warehouse Equipment		\$100,000.00
Gravy Preparation Equipment		\$100,000.00
Filling Equipment		\$150,000.00
Horizontal Form Fill Seal Equipment		\$350,000.00
First Inspection Equipment		\$10,000.00
Rack Loading Equipment		\$40,000.00
Retort Equipment		\$940,000.00
Rack Unloading Equipment		\$40,000.00
Final Inspection Equipment		\$10,000.00
Final Packaging Equipment		\$300,000.00
Total Purchased Equipment (PEC)		\$2,040,000.00

Installation	45.00% PEC	\$918,000.00
Instrumentation	9.00% PEC	\$183,600.00
Piping	10.00% PEC	\$204,000.00
Electrical	10.00% PEC	\$204,000.00
Service Facility	40.00% PEC	\$816,000.00
Engineering & Supervision	33.00% PEC	\$673,200.00
Total Direct Plant Cost (DPC)		\$5,038,800.00

Contingency	25.00% DPC	\$1,259,700.00
Fixed Capital Investment (FCI)		\$6,298,500.00

Working Capital	15.00% TCI	\$1,111,500.00
Total Capital Investment (TCI)		\$7,410,000.00

Assumptions Retort		
Containers/Rack	21	
Rack/Crate	27	
Crate/Retort	4	
Retort Load [container/retort]	2268	
Retort Cycle Time [min]	75	
Retort Capacity [cont/min]	30.24	
Number of Retorts	4	
Cost one retort	\$235,000.00	
Budget cost one 1100 retort	\$178,000.00	rotating
Budget cost one 1300 retort	\$235,000.00	rotating

Utility Cost Estimate

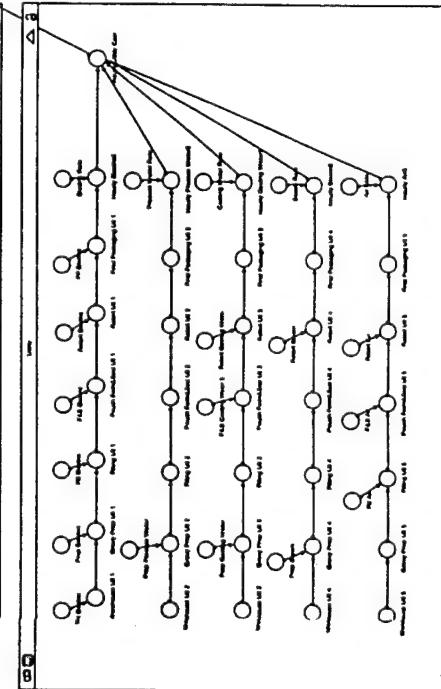
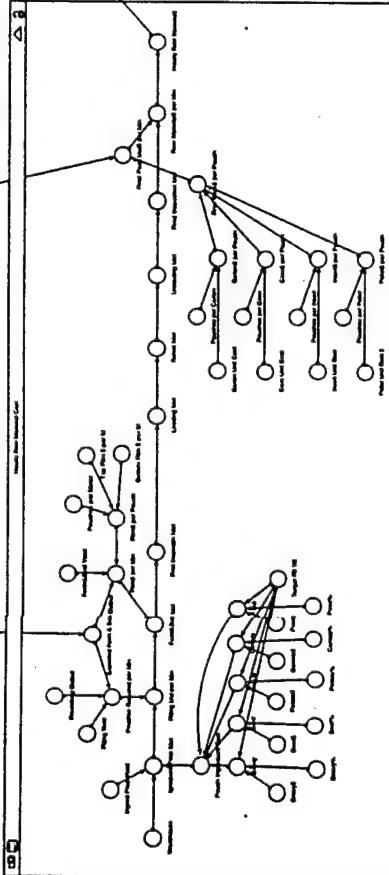
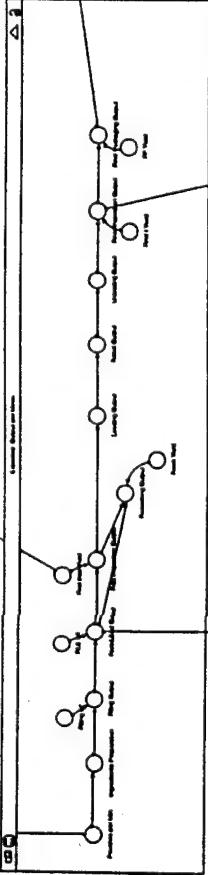
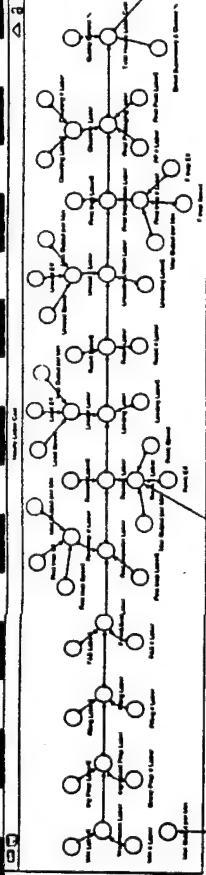
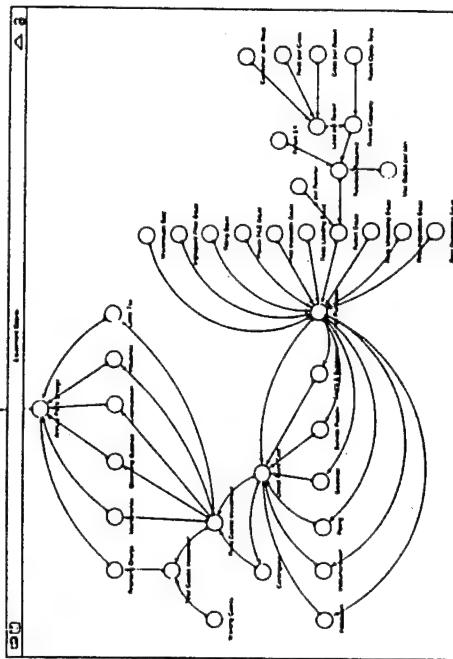
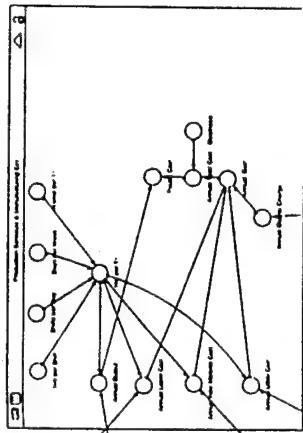
Equipment	Gas [ft ³ /hr]	Water (P) [gal/hr]	Water (C) [gal/hr]	Steam [lb/hr]	Air [ft ³ /hr]	Electric [kW]
Warehouse	0	0	0	0	0	25
Gravy Prep	0	200	200	500	0	5
Filling	0	0	0	0	10	10
Packaging	0	0	50	0	1000	20
Retorting	0	0	10000	3000	100	15
FP Packaging	0	0	0	0	0	10
Total	0	200	10250	3500	1110	85

	Units	Usage	Cost/Unit	\$/Hr
Natural Gas	[ft ³ /hr]	0	\$0.0050	\$0.000
Process Water	[gal/hr]	200	\$0.0010	\$0.200
Cooling Water	[gal/hr]	10250	\$0.0003	\$3.075
Steam	[lb/hr]	3500	\$0.0070	\$24.500
Compressed Air	[ft ³ /hr]	1110	\$0.0004	\$0.444
Electric	[kW]	85	\$0.0900	\$7.650
Energy Cost per Hour				\$35.869
Annual Energy Cost				\$68,868.480

Manufacturing Cost

Direct Production Cost		Annual Cost
Raw Materials		\$4,314,934
Pouch Packaging Cost		\$857,593
Carton & Case Cost		\$703,832
Total Annual Labor Cost		\$985,920
Utilities		\$68,868
		=====
Total Direct Production Cost		\$6,931,148
 Fixed Charges		
Depreciation	10.00% FCI	\$629,850
Maintenance and Repair	6.00% FCI	\$377,910
Operating Supplies	1.00% FCI	\$62,985
Local taxes	4.00% FCI	\$251,940
Insurance	1.00% FCI	\$62,985
Financing Cost	9.00% TCI	\$666,900
Rent		
		=====
Total Fixed Charges		\$2,052,570
Total Plant Overhead	7.00% TMC	\$676,194
		=====
Total Manufacturing Cost (TMC)		\$9,659,911
Manufacturing Cost per Packaging Unit		\$1.18

APPENDIX E
Visual Representation: Cost Analysis for Beef Stew Pouches



Equipment Capital

- $\$_per_Retorter = 235000.00$
- $Annual_Plant_Charge =$
 $Depreciation+Financing_Charge+Insurance+Local_Tax+Maintenance+Operating_Supplies$
- $Container_per_Rack = 21$
- $Contingency = Direct_Plant_Cost*0.25$

- $Crate_per_Retort = 4$
- $Depreciation = 0.10*Fixed_Capital_Investment$
- $Direct_Plant_Cost = Total_Purchase+Electrical++Eng'g \& Supervise+$
 $\cdot Installation+Instrumentation+Piping+Service_Facility$
- $Electrical = Total_Purchase*0.10$

- $Eng'g \& Supervise = Total_Purchase*0.33$

- $Filling_Equip = 350000$

- $Final_Inspection_Equip = 10000.00$

- $Final_Packaging_Equip = 300000.00$

- $Financing_Charge = 0.09*Total_Capital_Investment$
- $First_Inspectin_Equip = 0.00$

- $Fixed_Capital_Investment = Contingency+Direct_Plant_Cost$
- $Ingrediant_Prep_Equip = 100000.00$

- $Installation = Total_Purchase*.45$

- $Instrumentation = Total_Purchase*0.09$

- $Insurance = 0.01*Fixed_Capital_Investment$
- $Load_per_Retort = Container_per_Rack*Crate_per_Retort*Rack_per_Crate$
- $Local_Tax = 0.04*Fixed_Capital_Investment$
- $Maintenance = 0.06*Fixed_Capital_Investment$
- $Operating_Supplies = 0.01*Fixed_Capital_Investment$
- $Piping = Total_Purchase*0.10$

- $Pouch_F\&S_Equip = 540000$
- $Rack_Loading_Equip = 40000.00$

- $Rack_per_Crate = 27$
- $Rack_Unloading_Equip = 40000.00$

Retorters_Required = ROUND(Max_Output_per_Min/Retort_Capacity/Retort_Eff+0.5)
Retort_Capacity = Load_per_Retort/Retort_Cycle_Time
Retort_Cycle_Time = 75
Retort_Eff = 0.9
Retort_Equip = \$_per_Retorter*Retorters_Required
Service_Facility = Total_Purchase*.40

Total_Capital_Investment =
Fixed_Capital_Investment/(1-Working_Capital)*Working_Capital+Fixed_Capital_Investment

Total_Purchase =
Filling_Equip+Final_Inspection_Equip+Final_Packaging_Equip+First_Inspectin_Equip+Ingredgient_Prep_Equip+Pouch_F&S_Equip+Rack>Loading_Equip+Rack_Unloading_Equip+Retort_Equip+Warehouse_Equip

Warehouse_Eqip = 100000.00

Working_Capital = 0.15

Expected Output per Minite

F&S_Eff = 0.9

Filling_Eff = 0.95
Filling_Output = Ingredients_Preparation*Filling_Eff
Final_Inspection_Output = Unloading_Output*Final_I_Yield
Final_I_Yield = 0.98

Final_Packaging_Output = Final_Inspection_Output*FP_Yield
First_Inspection_Output = Form&Seal_Output*First_Insp_Yield
First_Insp_Yield = 0.8
Form&Seal_Output = Filling_Output*F&S_Eff
FP_Yield = 0.99
Ingredients_Preparation = Pouches_per_Min
Loading_Output = First_Inspection_Output
Pouches_per_Min = 102

Retort_Output = Loading_Output
Rework_Yield = 0.8

Reworking_Output = (Form&Seal_Output-First_Inspection_Output)*Rework_Yield
Unloading_Output = Retort_Output

Hourly Labor Cost

Cleaning_#_Labor = 3
Cleaning_Labor\$ = 10
Cleaning_Labor = Cleaning_#_Labor*Cleaning_Labor\$

- Direct_Supervisory_&_Clerical_% = 0.15
- F&S_#_Labor = 1
- F&S_Labor\$ = 15
- Filling_#_Labor = 4
- Filling_Labor = Filling_#_Labor*Filling_Labor\$+Ingredient_Prep_Labor
- Filling_Labor\$ = 10
- Final_Inspection_Labor = Unloading&Wash_Labor+Final_Insp_#_Labor*Final_Insp_Labor\$
- Final_Insp_#_Labor = ROUND(Max_Output_per_Min/F_Insp_Eff/F_Insp_Speed+0.5)
- Final_Insp_Labor\$ = 10
- Final_Packaging_Labor = FP_#_Labor*Final_Pack_Labor\$+Final_Inspection_Labor+Cleaning_Labor
- Final_Pack_Labor\$ = 10
- First_Inspectin_Labor = First_Insp_Labor\$*First_Insp_#_Labor+Form&Seal_Labor
- First_Insp_#_Labor = ROUND(Max_Output_per_Min/First_Insp_Eff/First_Insp_Speed+0.5)
- First_Insp_Eff = 0.9
- First_Insp_Labor\$ = 10
- First_Insp_Speed = 20
- Form&Seal_Labor = F&S_#_Labor*F&S_Labor\$+Filling_Labor
- FP_#_Labor = 2
- F_Insp_Eff = 0.9
- F_Insp_Speed = 10
- Gravy_Prep_#_Labor = 1
- Ingredient_Prep_Labor = Gravy_Prep_#_Labor*Ing_Prep_Labor\$+Warehouse_Labor
- Ing_Prep_Labor\$ = 10
- Loading_Labor = Rework_Labor+Load_#_Labor*Loading_Labor\$
- Loading_Labor\$ = 10
- Load_#_Labor = ROUND(Max_Output_per_Min/Load_Eff/Load_Speed+0.5)
- Load_Eff = 0.9
- Load_Speed = 30
- Max_Output_per_Min = Pouches_per_Min
- Quality_Control_% = 0.15
- Retort_#_Labor = 2
- Retort_Labor = Loading_Labor+Retort_#_Labor*Retort_Labor\$
- Retort_Labor\$ = 15
- Rewk_#_Labor = ROUND(Max_Output_per_Min*(1-First_Insp_Yield)/Rewk_Eff/Rewk_Speed + 0.5)
- Rewk_Eff = 0.9
- Rewk_Speed = 10
- Rework_Labor = First_Inspectin_Labor+Rewk_#_Labor*Rework_Labor\$
- Rework_Labor\$ = 10
- Total_Hourly_Labor_Cost =

$$\text{Final_Packaging_Labor} * (1 + \text{Direct_Supervisory_Clerical_ \% } + \text{Quality_Control_ \% })$$

Unloading&Wash_Labor = Retort_Labor+Unload_#_Labor*Unloading_Labor\$
Unloading_Labor\$ = 10
Unload_#_Labor = ROUND(Max_Output_per_Min/Unload_Eff/Unload_Speed+0.5)
Unload_Eff = 0.9
Unload_Speed = 40
Warehouse_Labor = WH_Labor\$*WH_#_Labor
WH_#_Labor = 2
WH_Labor\$ = 10

Hourly Raw Material Cost

Beef = Target_Fill_Wt*Beef%*Beef\$
Beef\$ =
•2.00/28.3/16

Beef% = 0.3948

Bottom_Film\$_per_M = 0.71

Carrots = Target_Fill_Wt*Carrots%*Carrots\$

Carrots\$ = 0.65/28.3/16

Carrots% = 0.073

Carton\$_per_Pouch = Carton_Unit_Cost/Pouches_per_Carton

Carton_Unit_Cost = 0.07

Case\$_per_Pouch = Case_Unit_Cost/Pouches_per_Case

Case_Unit_Cost = 0.34

Expected_Form_&_Seal_Output = Form&Seal_Output

Filling_Mat_per_Min = Ingredient_Prep_Mat*Pouches_Required_per_Min

Filling_Yield = 0.97

Film\$_per_Min = Film\$_per_Pouch*Expected_Form_&_Seal_Output/Form&Seal_Yield

Film\$_per_Pouch = (Bottom_Film\$_per_M+Top_Film\$_per_M)/Pouches_per_Meter

Final_Inspection_Mat = Unloading_Mat

Final_Pack\$_per_Pouch =

Carton\$_per_Pouch+Case\$_per_Pouch+Insert\$_per_Pouch+Pallet\$_per_Pouch

Final_Pack_Mat\$_per_Min = Final_Inspection_Output*Final_Pack\$_per_Pouch

First_Inspectin_Mat = Form&Seal_Mat

Form&Seal_Mat = Filling_Mat_per_Min+Film\$_per_Min

Form&Seal_Yield = 0.98

Gravy = Target_Fill_Wt*Gravy%*Gravy\$

Gravy\$ = 0.15/28.3/16

Gravy% = 0.4292

Hourly_Raw_Material\$ = Raw_Material\$_per_Min*60

Ingredient_Prep_Mat = Warehouse+Pouch_Ingredient_Cost/Ingred_Prep_Yield

Ingred_Prep_Yield = 0.95

Insert\$_per_Pouch = Insert_Unit_Cost/Pouches_per_Insert

Insert_Unit_Cost = 0.23

Loading_Mat = First_Inspectin_Mat

Pallet\$_per_Pouch = Pallet_Unit_Cost_2/Pouches_per_Pallet

- Pallet_Unit_Cost_2 = 10.0
- Peas = Target_Fill_Wt*Peas%*Peas\$
- Peas\$ = 0.85/28.3/16
- Peas% = 0.03
- Potato = Target_Fill_Wt*Potato%*Potato\$
- Potato\$ = 0.70/28.3/16
- Potato% = 0.073
- Pouches_per_Carton = 1
- Pouches_per_Case = 72
- Pouches_per_Insert = 72
- Pouches_per_Meter = 16.52893
- Pouches_per_Pallet = 2880
- Pouches_Required_per_Min = Expected_Form_&_Seal_Output/Filling_Yield-Reworking_Output
- Pouch_Ingredient_Cost = Beef+Carrots+Gravy+Peas+Potato
- Raw_Material\$_per_Min = Final_Inspection_Mat+Final_Pack_Mat\$_per_Min
- Retort_Mat = Loading_Mat
- Target_Fill_Wt = 233
- Top_Film_\$_per_M = 0.71
- Unloading_Mat = Retort_Mat
- Warehouse = 0.0

Production Schedule & Manufacturing Cost

- Annual_Capital_Charge = Annual_Plant_Charge
- Annual_Labor_Cost = Total_Hourly_Labor_Cost*Hrs_per_Yr
- Annual_Output = Final_Packaging_Output*60*Hrs_per_Yr
- Annual_Raw_Material_Cost = Hourly_Raw_Material\$*Hrs_per_Yr
- Annual_Total_Cost = Annual__Cost/(1-Overhead)*Overhead+Annual__Cost
- Annual.Utility_Cost = Hourly.Utility_Cost*Hrs_per_Yr
- Annual__Cost =
 - Annual_Capital_Charge+Annual_Labor_Cost+Annual_Raw_Material_Cost+Annual.Utility_Cost
- Days_per_Week = 5
- Hrs_per_Shift = 8
- Hrs_per_Yr = Days_per_Week*Hrs_per_Shift*Shifts_per_Day*Weeks_per_Yr
- Overhead = .07
- Pouch_Cost = Annual_Total_Cost/Annual_Output
- Shifts_per_Day = 1
- Weeks_per_Yr = 48

Utility

- Air_Rate = 0.0004
- Cooling_Water_Rate = 0.0003
- Electric_Rate = 0.09
- F&S_Air = 1000

F&S_Cooling_Water_3 = 50
F&S_Electric = 20
Filling_Utl_1 = Fill_Electric+Gravy_Prep_Utl_1
Filling_Utl_2 = Gravy_Prep_Utl_2
Filling_Utl_3 = Gravy_Prep_Utl_3
Filling_Utl_4 = Gravy_Prep_Utl_4
Filling_Utl_5 = Gravy_Prep_Utl_5+Fill_Air
Fill_Air = 10
Fill_Electric = 10
Final_Packaging_Utl_1 = FP_Electric+Retort_Utl_1
Final_Packaging_Utl_2 = Retort_Utl_2
Final_Packaging_Utl_3 = Retort_Utl_3
Final_Packaging_Utl_4 = Retort_Utl_4
Final_Packaging_Utl_5 = Retort_Utl_5
FP_Electric = 10
Gravy_Prep_Utl_1 = Prep_Electric+Warehouse_Utl_1
Gravy_Prep_Utl_2 = Prep_Process_Water+Warehouse_Utl_2
Gravy_Prep_Utl_3 = Prep_Cooling_Water+Warehouse_Utl_3
Gravy_Prep_Utl_4 = Warehouse_Utl_4+Prep_Steam
Gravy_Prep_Utl_5 = Warehouse_Utl_5
Hourly_Air\$ = Final_Packaging_Utl_5*Air_Rate
Hourly_Cooling_Water\$ = Cooling_Water_Rate*Final_Packaging_Utl_3
Hourly_Electric\$ = Electric_Rate*Final_Packaging_Utl_1
Hourly_Process_Water\$ = Final_Packaging_Utl_2*Process_Water_Rate
Hourly_Steam\$ = Final_Packaging_Utl_4*Steam_Rate
Hourly_Utility_Cost =
Hourly_Steam\$+Hourly_Air\$+Hourly_Cooling_Water\$+Hourly_Electric\$+Hourly_Process_Water\$
Pouch_Form&Seal_Utl_1 = F&S_Electric+Filling_Utl_1
Pouch_Form&Seal_Utl_2 = Filling_Utl_2
Pouch_Form&Seal_Utl_3 = F&S_Cooling_Water_3+Filling_Utl_3
Pouch_Form&Seal_Utl_4 = Filling_Utl_4
Pouch_Form&Seal_Utl_5 = Filling_Utl_5+F&S_Air
Prep_Cooling_Water = 200
Prep_Electric = 5
Prep_Process_Water = 200
Prep_Steam = 500
Process_Water_Rate = 0.001
Retort_Air = 100
Retort_Cooling_Water = 10000
Retort_Electric = 15
Retort_Steam = 3000
Retort_Utl_1 = Pouch_Form&Seal_Utl_1+Retort_Electric
Retort_Utl_2 = Pouch_Form&Seal_Utl_2
Retort_Utl_3 = Pouch_Form&Seal_Utl_3+Retort_Cooling_Water
Retort_Utl_4 = Pouch_Form&Seal_Utl_4+Retort_Steam

- Retort_Utl_5 = Retort_Air+Pouch_Form&Seal_Utl_5
- Steam_Rate = 0.007
- Warehouse_Utl_1 = WH_Electric
- Warehouse_Utl_2 = 0.0
- Warehouse_Utl_3 = 0.0
- Warehouse_Utl_4 = 0.0
- Warehouse_Utl_5 = 0.0

- WH_Electric = 25

APPENDIX F
SpreadSheet for Beef Stew Fill Weight Design B

Production Schedule

Hours/Shift	8
Shifts/Day	1
Days/Week	5
Weeks/Year	48
Hours/Year	1920

Production Rate MRE Line

Units/Minute	102
--------------	-----

Avg Unit Fill&Seal/Hour	4,651
Avg Unit for Fill / Hour with rework	4,455
Avg Unit FP Output Rate/Hour	4,250
Daily Unit Rate	34,001
Annual Output from Final Inspect	8,242,671
Annualized Unit Rate	8,160,244
Annual Requirement	5,000,000
Plant Utilization	61.27%

Process Yield & Efficiency

	Efficiency	Yield
Product Preparation Equipm.	90.0%	95.0% (yield of gravy system)
Filling Equipment	95.0%	97.0% (avg yield of product)
Horizontal Form & Seal Equipment	80.0%	90.0% (yield of packaging material)
Pouch Packaging System	76.0%	
First Inspection Equipment	90.0%	92.3% (% accepted pouches)
Rework System	80.0%	95.0%
Rack Loading Equipment	90.0%	100.0%
Retort Equipment	90.0%	100.0%
Rack Unloading Equipment	90.0%	100.0%
Final Inspection Equipment	90.0%	100.0% (% accepted pouches)
Final Packaging Equipment	70.0%	99.0% (% yield including qc samples to)

	Rated Capacity	Output Expected
Process Design Capacity		
Product Preparation Equipment	86.6	74.1 pouches/min
Filling Equipment	102.0	77.5 pouches/min
Horizontal Form & Seal Equipment	102.0	77.5 pouches/min
First Inspection Equipment	113.3	71.6 inspections/min
Rework System	9.8	5.7
Rack Loading Equipment	113.3	71.6 pouches/min
Retort Equipment	113.3	71.6 pouches/min
Rack Unloading Equipment	113.3	71.6 pouches/min
Final Inspection Equipment	113.3	71.6 inspections/min
Final Packaging Equipment	145.7	70.8 pouches/min

Material Data Cost Sheet

Formula	% Formula	Preparation			Drained Wt.		
		Yield%	Cost/lb	Cost/Lb	Fat Cont%	Salt Cont%	Yield%
95	41.13%	95.00%	\$0.15	\$0.065	3.60%	0.12%	
87	37.66%	95.00%	\$2.00	\$0.793	0.65%	2.36%	85.00%
49	21.21%						135.00%
20.473538	8.86%	95.00%	\$0.70	\$0.065			
20.473538	8.86%	95.00%	\$0.65	\$0.061			
8.0529248	3.49%	95.00%	\$0.85	\$0.031			
<hr/>				<hr/>			
231	100.00%			\$1.015			

Avg Target Fill Weight [gram] 231
[lb] 0.510159

Product Cost/Contain **\$0.518**

Material

\$/m	pouches/m	% yield	\$/pouch
\$0.71	16.528926	90.0%	\$0.048
\$0.71	16.528926	90.0%	\$0.048
<hr/>			
Pouch Cost			\$0.096

\$/unit	pouch/unit	% yield	\$/pouch
\$0.07	1	99.00%	\$0.074
\$0.34	72	99.00%	\$0.005
\$0.23	72	99.00%	\$0.003
\$10.00	2880	99.00%	\$0.003
<hr/>			
FP Packaging Cost			\$0.085

Labor Cost Estimate

		Rate	Wages
Warehouse Labor	2	\$10.00	\$20.00
Gravy Prep Labor	1	\$10.00	\$10.00
Filling Labor	1	\$10.00	\$10.00
Packaging Labor	1	\$15.00	\$15.00
First Inspection	6	\$10.00	\$60.00
Rework Labor	1	\$10.00	\$10.00
Rack Loading	4	\$10.00	\$40.00
Retort Labor	2	\$15.00	\$30.00
Rack Unloading & Washing	3	\$10.00	\$30.00
Final Inspection Labor	12	\$10.00	\$120.00
Finished Product Packaging	2	\$10.00	\$20.00
Cleaning Labor	3	\$10.00	\$30.00
===== ===== ===== =====			
Total Labor / Hr	38		\$395.00

Annual Opperating Labor Cost		\$758,400.00
Direct Supervisory and Clerical I	15.00% OL	\$113,760
Quality Control	15.00% OL	\$113,760
===== ===== =====		
Total Annual Labor Cost		\$985,920

Assumptions Labor:	sec/inspec	inspector
First Inspection Time	3	5.7
Second Inspection Time	6	11.3
===== ===== =====		
	p/man/min	man
Rack Loading	30	3.8
Rack Unloading	40	2.8
===== ===== =====		
	p/man/min	
Rework Labor	10	1.0

Capital Equipment

Warehouse Equipment		\$100,000.00
Gravy Preparation Equipment		\$100,000.00
Filling Equipment		\$150,000.00
Horizontal Form Fill Seal Equipment		\$350,000.00
First Inspection Equipment		\$10,000.00
Rack Loading Equipment		\$40,000.00
Retort Equipment		\$940,000.00
Rack Unloading Equipment		\$40,000.00
Final Inspection Equipment		\$10,000.00
Final Packaging Equipment		\$300,000.00
<hr/>		
Total Purchased Equipment (PEC)		\$2,040,000.00
<hr/>		
Installation	45.00% PEC	\$918,000.00
Instrumentation	9.00% PEC	\$183,600.00
Piping	10.00% PEC	\$204,000.00
Electrical	10.00% PEC	\$204,000.00
Service Facility	40.00% PEC	\$816,000.00
Engineering & Supervision	33.00% PEC	\$673,200.00
<hr/>		
Total Direct Plant Cost (DPC)		\$5,038,800.00
<hr/>		
Contingency	25.00% DPC	\$1,259,700.00
<hr/>		
Fixed Capital Investment (FCI)		\$6,298,500.00
<hr/>		
Working Capital	15.00% TCI	\$1,111,500.00
<hr/>		
Total Capital Investment (TCI)		\$7,410,000.00

Assumptions Retort		
Containers/Rack	21	
Rack/Crate	27	
Crate/Retort	4	
Retort Load [container/retort]	2268	
Retort Cycle Time [min]	75	
Retort Capacity [cont/min]	30.24	
Number of Retorts	4	
Cost one retort	\$235,000.00	
<hr/>		
Budget cost one 1100 retort	\$178,000.00	rotating
Budget cost one 1300 retort	\$235,000.00	rotating

Utility Cost Estimate

Equipment	Gas [ft ³ /hr]	Water (P) [gal/hr]	Water (C) [gal/hr]	Steam [lb/hr]	Air [ft ³ /hr]	Electric [kW]
Warehouse	0	0	0	0	0	25
Gravy Prep	0	200	200	500	0	5
Filling	0	0	0	0	10	10
Packaging	0	0	50	0	1000	20
Retorting	0	0	10000	3000	100	15
FP Packaging	0	0	0	0	0	10
Total	0	200	10250	3500	1110	85

	Units	Usage	Cost/Unit	\$/Hr
Natural Gas	[ft ³ /hr]	0	\$0.0050	\$0.000
Process Water	[gal/hr]	200	\$0.0010	\$0.200
Cooling Water	[gal/hr]	10250	\$0.0003	\$3.075
Steam	[lb/hr]	3500	\$0.0070	\$24.500
Compressed Air	[ft ³ /hr]	1110	\$0.0004	\$0.444
Electric	[kW]	85	\$0.0900	\$7.650
Energy Cost per Hour				\$35.869
Annual Energy Cost				\$68,868

Manufacturing Cost

Direct Production Cost		Annual Cost
Raw Materials		\$4,428,820
Pouch Packaging Cost		\$857,593
Carton & Case Cost		\$703,832
Total Annual Labor Cost		\$985,920
Utilities		\$68,868
	=====	
Total Direct Production Cost		\$7,045,034
Fixed Charges		
Depreciation	10.00% FCI	\$629,850
Maintenance and Repair	6.00% FCI	\$377,910
Operating Supplies	1.00% FCI	\$62,985
Local taxes	4.00% FCI	\$251,940
Insurance	1.00% FCI	\$62,985
Financing Cost	9.00% TCI	\$666,900
Rent		
	=====	
Total Fixed Charges		\$2,052,570
Total Plant Overhead	7.00% TMC	\$684,766
	=====	
Total Manufacturing Cost (TMC)		\$9,782,370
Manufacturing Cost per Packaging Unit		\$1.20

Process Capability Index for The First Major Quality Characteristic: Beef Drained Weight									
Characteristic	1. Variable 2. Attribute	1. Stationary 2. Non-stationary	1. Bilateral Specs 2. Unilateral Specs	1. Symmetric Specs 2. Asymmetric Specs	Target Value	Avg. Lower Spec.	Variable Characteristics Ind. Lower Spec.	Attribute Characteristics Sample Size	Estimated PCI
Beef Dr. Wt.	1	1	2	1	73.95	68	50.7	17	55.4
									51
									48.8
									45.6
									41.8
									34.4
									41.8
									45
									40.2
									47
									52
									43
									45.4
									47
									43.8
									55.3
									40.4
									1.281094122
									4.48835935
									17.25
									5.55
									73.95
									1

Process Capability Index for The First Critical Quality Characteristic: Net Weight

Process Capability Index for The last Major Quality Characteristic: Vegetables Drained Weight									
Characteristics	1. Variable	2. Attribute	1. Stationary	2. Non-stationary	1. Bilateral Specs		2. Asymmetrical Specs		Attribute Characteristics
					Ind. Lower Spec.	Avg. Lower Spec.	Target Value	Ind. Upper Spec.	
Vegetable Dr. Wt.	1	1	2	1	34	45.3	66.15	55.3	40.5
					17				61.6
									58.2
									52.8
									67.5
									49.8
									60
									47.5
									63.3
									52.5
									62
									68
									47
									54
									67.3
									63
									61.2
									1.286498274
					32.15	8.330105748	61.2		
					20.65	66.15			

Producibility Index

		Importance Ratio
Minimum Critical PCI:	1.385690321	
Geomean Critical PCI:	1.385690321	5
Minimum Major PCI:	1.120084712	
Geomean Major PCI:	1.254564171	3
Minimum Minor PCI:	3.412348722	
Geomean Minor PCI:	3.412348722	1
Average Overall PCI:	1.481707748	

Producibility Index	PCI Critical:	1.385690321
	PCI Major:	1.120084712
	PCI Minor:	3.412348722
	PCI Average:	1.481707748
	Manufacturing Cost:	\$1.199

APPENDIX G
SpreadSheet for Ham Slice Pouch Design B

Production Schedule

Hours/Shift	8
Shifts/Day	1
Days/Week	5
Weeks/Year	48
Hours/Year	1920
Production Rate MRE Line	
Units/Minute	60
Avg Unit Fill&Seal/Hour	2,924
Avg Unit for Fill / Hour with rework	2,798
Avg Unit FP Output Rate/Hour	2,705
Daily Unit Rate	21,643
Annual Output from Final Inspection	5,246,874
Annualized Unit Rate	5,194,405
Annual Requirement	5,000,000
Plant Utilization	96.26%

Process Yield & Efficiency

	Efficiency	Yield	
Slicing Operation	90.0%	90.0% (yield of gravy system)	
Robot/Manual Fill	95.0%	99.0% (avg yield of product)	
Horizontal Form & Seal Equipment	95.0%	98.0% (yield of packaging material)	
Pouch Packaging System	81.2%		
First Inspection Equipment	90.0%	94.4% (% accepted pouches)	
Rework System	80.0%	95.0%	
Rack Loading Equipment	90.0%	100.0%	
Retort Equipment	90.0%	100.0%	
Rack Unloading Equipment	90.0%	100.0%	
Final Inspection Equipment	90.0%	99.0% (% accepted pouches)	
Final Packaging Equipment	70.0%	99.0% (% yield including qc samples to)	

	Rated Capacity	Output Expected	
Process Design Capacity			
Product Preparation Equipment	57.5	46.6 pouches/min	
Filling Equipment	60.0	48.7 pouches/min	
Horizontal Form & Seal Equipment	60.0	48.7 pouches/min	
First Inspection Equipment	66.7	46.0 inspections/min	
Rework System	4.2	2.6	
Rack Loading Equipment	66.7	46.0 pouches/min	
Retort Equipment	66.7	46.0 pouches/min	
Rack Unloading Equipment	66.7	46.0 pouches/min	
Final Inspection Equipment	66.7	45.5 inspections/min	
Final Packaging Equipment	85.7	45.1 pouches/min	

Material Data Cost Sheet

Product Ingredient	Formula	% Formula	%yield	Cost/lb	Cost/Lb	Fat Cont%	Salt Cont%	Yield%
Ham	150	100.00%	90.00%	\$1.70	\$1.889	4.83%	2.06%	85.00%
	=====	=====			=====			
	150	100.00%			\$1.889			

Avg Target Fill Weight [gram]
[lb] 150
0.3312721

Product Cost/Contain **\$0.626**

Packaging Material

	\$/m	pouches/m	% yield	\$/pouch
Top Film	\$0.71	16.528926	98.0%	\$0.044
Bottom Film	\$0.71	16.528926	98.0%	\$0.044
			=====	
		Pouch Cost		\$0.088

	\$/unit	pouch/unit	% yield	\$/pouch
Carton	\$0.07	1	99.00%	\$0.074
Case	\$0.34	72	99.00%	\$0.005
Inserts	\$0.23	72	99.00%	\$0.003
Pallet	\$10.00	2880	99.00%	\$0.003
			=====	
		FP Packaging Cost		\$0.085

Labor Cost Estimate

		Rate	Wages
Warehouse Labor	2	\$10.00	\$20.00
Ham Unpacking/Slicing	2	\$10.00	\$20.00
Filling Labor	2	\$10.00	\$20.00
Tiromat Operating Labor	1	\$15.00	\$15.00
First Inspection	4	\$10.00	\$40.00
Rework Labor	1	\$10.00	\$10.00
Rack Loading	3	\$10.00	\$30.00
Retort Labor	3	\$15.00	\$45.00
Rack Unloading & Washing	2	\$10.00	\$20.00
Final Inspection Labor	7	\$10.00	\$70.00
Finished Product Packaging	2	\$10.00	\$20.00
Cleaning Labor	3	\$10.00	\$30.00
=====			
Total Labor / Hr	32		\$340.00

Annual Opperating Labor Cost		\$652,800
Direct Supervisory and Clerical I	15.00% OL	\$97,920
Quality Control	15.00% OL	\$97,920
=====		
Total Annual Labor Cost		\$848,640

Assumptions Labor:	sec/inspec	inspector
First Inspection Time	3	3.3
Second Inspection Time	6	6.7
p/man/min		
Rack Loading	30	2.2
Rack Unloading	40	1.7
p/man/min		
Rework Labor	10	0.4

Capital Equipment

Warehouse Equipment		\$100,000.00
Slicer/Unpacking Equipment		\$100,000.00
Filling Equipment: Robot		\$0.00
Horizontal Form Fill Seal Equipment		\$350,000.00
First Inspection Equipment		\$0.00
Rack Loading Equipment		\$40,000.00
Retort Equipment		\$705,000.00
Rack Unloading Equipment		\$40,000.00
Final Inspection Equipment		\$10,000.00
Final Packaging Equipment		\$300,000.00
<hr/>		
Total Purchased Equipment (PEC)		\$1,645,000.00

Installation	45.00% PEC	\$740,250.00
Instrumentation	9.00% PEC	\$148,050.00
Piping	10.00% PEC	\$164,500.00
Electrical	10.00% PEC	\$164,500.00
Service Facility	40.00% PEC	\$658,000.00
Engineering & Supervision	33.00% PEC	\$542,850.00
<hr/>		

Total Direct Plant Cost (DPC)		\$4,063,150.00
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Contingency	25.00% DPC	\$1,015,787.50
<hr/>		

Fixed Capital Investment (FCI)		\$5,078,937.50
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Working Capital	15.00% TCI	\$896,283.09
<hr/>		

Total Capital Investment (TCI)		\$5,975,220.59
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Assumptions Retort		
Containers/Rack	21	
Rack/Crate	27	
Crate/Retort	4	
Retort Load [container/retort]	2268	
Retort Cycle Time [min]	75	
Retort Capacity [cont/min]	30.24	
Number of Retorts	3	
Cost one retort	\$235,000.00	
<hr/>		
Budget cost one 1100 retort	\$178,000.00	rotating
Budget cost one 1300 retort	\$235,000.00	rotating

Utility Cost Estimate

Equipment	Gas [ft ³ /hr]	Water (P) [gal/hr]	Water (C) [gal/hr]	Steam [lb/hr]	Air [ft ³ /hr]	Electric [kW]
Warehouse	0	0	0	0	0	25
Ham Slicer	0	0	0	0	0	5
Filling: Robot	0	0	0	0	0	0
Packaging	0	0	50	0	1000	20
Retorting	0	0	10000	3000	100	15
FP Packaging	0	0	0	0	0	10
Total	0	0	10050	3000	1100	75

	Units	Usage	Cost/Unit	\$/Hr
Natural Gas	[ft ³ /hr]	0	\$0.0050	\$0.000
Process Water	[gal/hr]	0	\$0.0010	\$0.000
Cooling Water	[gal/hr]	10050	\$0.0003	\$3.015
Steam	[lb/hr]	3000	\$0.0070	\$21.000
Compressed Air	[ft ³ /hr]	1100	\$0.0004	\$0.440
Electric	[kW]	75	\$0.0900	\$6.750
Energy Cost per Hour				\$31.205
Annual Energy Cost				\$59,914

Manufacturing Cost

Direct Production Cost	Annual Cost
Raw Materials	\$3,361,644
Pouch Packaging Cost	\$495,136
Carton & Case Cost	\$448,025
Total Annual Labor Cost	\$848,640
Utilities	\$59,914
<hr/>	
Total Direct Production Cost	\$5,213,359

Fixed Charges		
Depreciation	10.00% FCI	\$507,894
Maintenance and Repair	6.00% FCI	\$304,736
Operating Supplies	1.00% FCI	\$50,789
Local taxes	4.00% FCI	\$203,158
Insurance	1.00% FCI	\$50,789
Financing Cost	9.00% TCI	\$537,770
Rent		
<hr/>		
Total Fixed Charges		\$1,655,136

Total Plant Overhead	7.00% TMC	\$516,983
Total Manufacturing Cost (TMC)		\$7,385,478

Manufacturing Cost per Packaging Unit	\$1.422
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Process Capability Index for The First Critical Quality Characteristic: Net Weight

Process Capability Index for The First Critical Quality Characteristic: Net Weight									
Characteristics	1. Variable 2. Attribute	1. Stationary 2. Non-stationary	1. Bilateral Specs 2. Unilateral Specs	1. Symmetric Specs 2. Asymmetric Specs		Target Value	Upper Spec Unit	Lower Spec Unit	Variable Characteristics
				1	2				
						150	160	140	Attribute Characteristics
								10	Sample Size
								32	Number of Defects
								42	Sample Size
								38	Number of Defects
								40	Sample Size
								35	Number of Defects
								46	Sample Size
								40	Number of Defects
								38	Sample Size
								35	Number of Defects
								42	Sample Size
								30	Number of Defects
								30	Sample Size
								3.19858164	Net Weight
								42	Attribute Characteristics
								3.1260775	Estimated PCI

Process Capability Index for The First Major Quality Characteristic: Hard Drained Weight													
Characteristics	1. Variable	2. Attribute	1. Stationary	2. Non-stationary	1. Bilateral Specs			2. Unilateral Specs			Attribute Characteristics	Number of Defects	Estimated PCL
					Target Value	Avg. Lower Spec.	Variability	Ind. Lower Spec.	Ind. Upper Spec.	Sample Size			
Hard Drained Wt.	1	1	1	2	127.5	102.1	107.7	107.7	107.7	10	91	103	
											94		
											97		
											91		
											102		
											88		
											95		
											102		
											1,128026501		

Process Capability Index for The First Critical Quality Characteristic: Net Weight											
Characteristic	1. Variable 2. Attribute	1. Stationary 2. Non-stationary	1. Bilateral Specs 2. Unilateral Specs	1. Symmetric Specs		2. Asymmetric Specs		Variable Characteristics			Attribute Characteristics Number of Defects Sample Size
				Target Value	Avg. Value	Ind. Lower Spec.	Avg. Lower Spec.	Sample Size	Sample Data		
Net Weight1	1	2	1	150	127.6	113.4	10	160			
								153			
								159			
								149			
								147			
								152			
								151			
								151			
								161			
								167			
								1565046000			
				150	22.4	36.6	7795297726				

Producibility Index

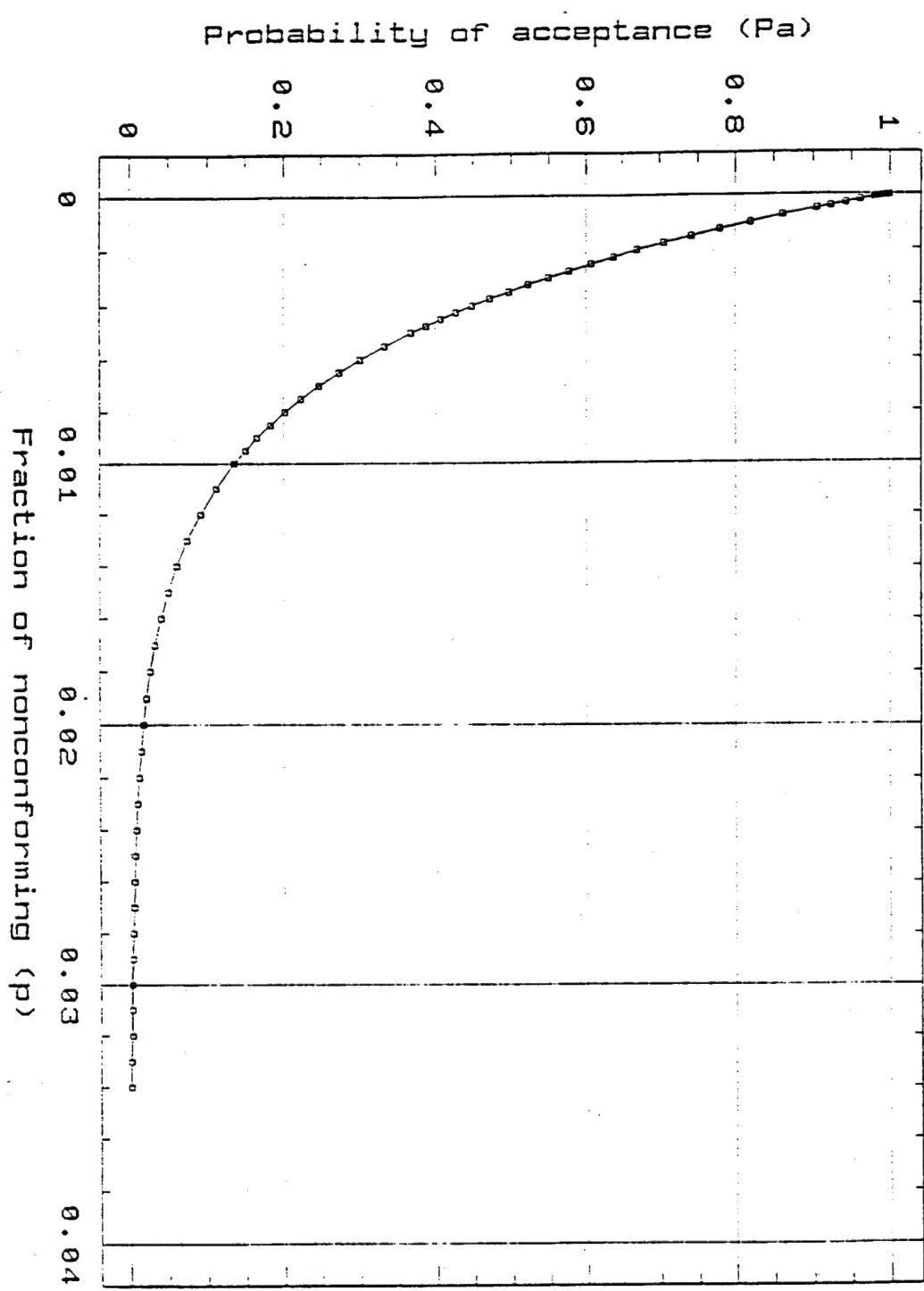
		Importance Ratio
Minimum Critical PCI:	1.09799051	
Geomean Critical PCI:	1.852656963	5
Minimum Major PCI:	1.128026601	
Geomean Major PCI:	1.328688672	3
Minimum Minor PCI:		
Geomean Minor PCI:		1
Average Overall PCI:	1.635519006	

Producibility Index

PCI Critical:	1.09799051
PCI Major:	1.128026601
PCI Minor:	
PCI Average:	1.635519006
Manufacturing Cost:	\$1.422

APPENDIX H
Operating Characteristics Curve and Cross Reference Table for
Pouch Defect Military Sampling Plan

OC curve for sampling plan, $n=209$ $c=0$



Nonconforming Fraction vs. Acceptance Probability
for Sampling Plan, n=209 c=0

row	p	Pa	row	p	Pa
1	0.000005	0.999	35	0.006000	0.301
2	0.000010	0.998	36	0.006500	0.273
3	0.000020	0.996	37	0.007000	0.247
4	0.000030	0.994	38	0.007500	0.223
5	0.000040	0.992	39	0.008000	0.202
6	0.000050	0.990	40	0.008500	0.183
7	0.000060	0.988	41	0.009000	0.165
8	0.000070	0.986	42	0.009500	0.150
9	0.000080	0.984	43	0.010000	0.135
10	0.000090	0.982	44	0.011000	0.111
11	0.000100	0.980	45	0.012000	0.091
12	0.000200	0.961	46	0.013000	0.074
13	0.000300	0.942	47	0.014000	0.061
14	0.000400	0.923	48	0.015000	0.050
15	0.000500	0.905	49	0.016000	0.041
16	0.000750	0.861	50	0.017000	0.033
17	0.001000	0.819	51	0.018000	0.027
18	0.001250	0.779	52	0.019000	0.022
19	0.001500	0.741	53	0.020000	0.018
20	0.001750	0.705	54	0.021000	0.015
21	0.002000	0.670	55	0.022000	0.012
22	0.002250	0.638	56	0.023000	0.010
23	0.002500	0.607	57	0.024000	0.008
24	0.002750	0.577	58	0.025000	0.007
25	0.003000	0.549	59	0.026000	0.006
26	0.003250	0.522	60	0.027000	0.005
27	0.003500	0.497	61	0.028000	0.004
28	0.003750	0.472	62	0.029000	0.003
29	0.004000	0.449	63	0.030000	0.002
30	0.004250	0.427	64	0.031000	0.002
31	0.004500	0.407	65	0.032000	0.002
32	0.004750	0.387	66	0.033000	0.001
33	0.005000	0.368	67	0.034000	0.001
34	0.005500	0.333			